

# **Minimum Energy Method for Resolving the Azimuthal Ambiguity in Hinode/SOT Vector Magnetogram Data**

**K. D. Leka**

**Graham Barnes**

**Ashley Crouch**

NorthWest Research Associates

Boulder, Colorado

- A fast, Fortran code for solving the  $180^\circ$  azimuthal-angle ambiguity.
- Based on the “minimum-energy” approach, best-performing in numerous objective model-based tests.
- Available at: [www.cora.nwra.com/AMBIG/](http://www.cora.nwra.com/AMBIG/)

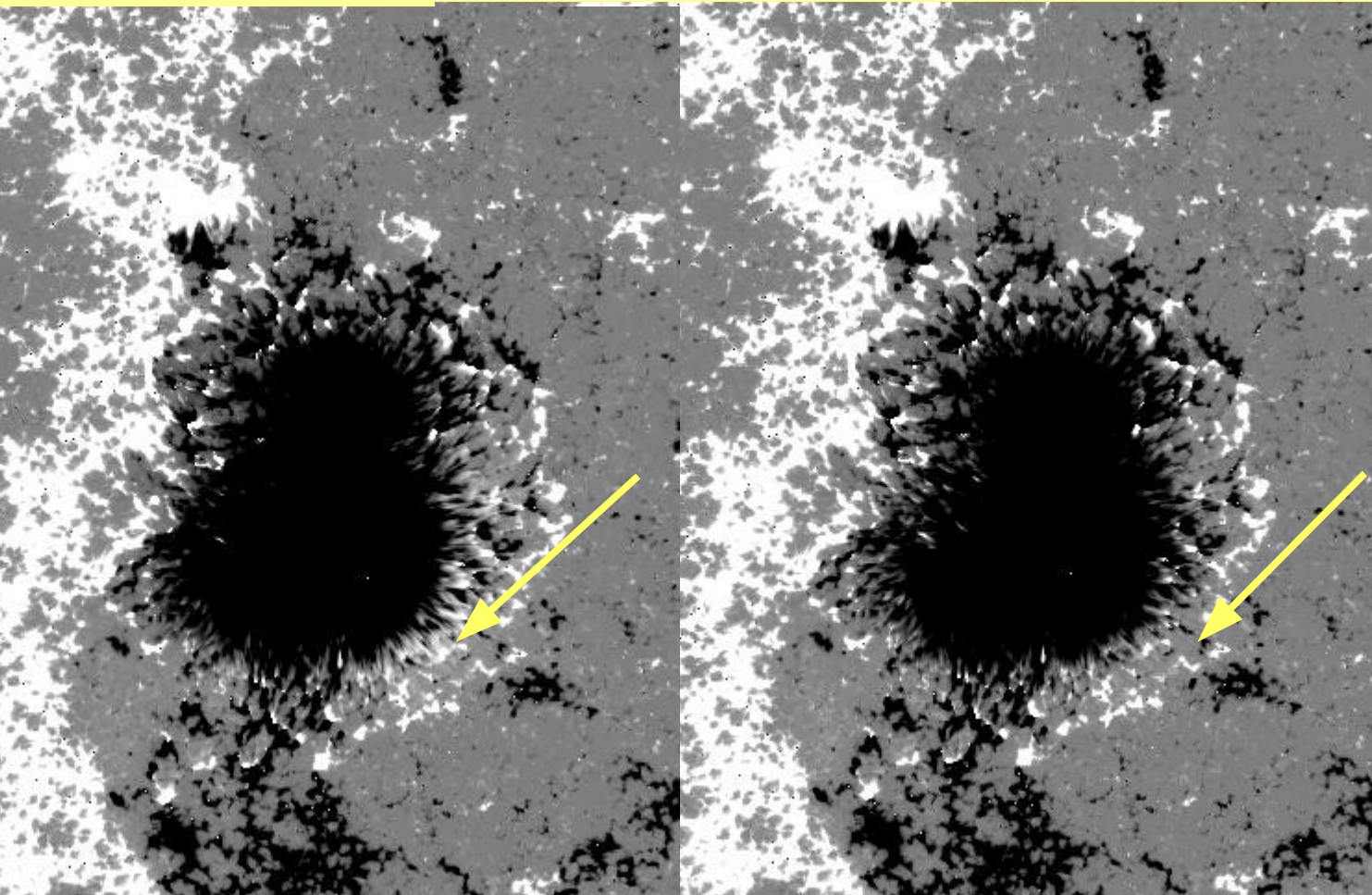
- **GOAL: automated algorithm with high “performance value”**

(courtesy C. Henney):

- *Accurate enough for science goals, fast enough for large data sets*
  - Stable for conditions of interest (e.g. Quiet areas, complex groups)
  - Fast relative to inversion time,  
(define  $\text{Time} = \text{InversionTime} / \text{AmbigTime}$ )
  - Is the algorithm automatic?  
If yes, (set  $\text{Auto} = 1$ , otherwise  $\text{Auto} = \infty$ )
- **$\text{Merit} = (\% \text{ accuracy} * \text{Stability} + \text{Time}) / \text{Auto}$**

- **Assume an inversion procedure:**

- **I, Q, U, V spectra  $\rightarrow B_{\text{los}}, B_{\text{trans}}, \phi$  (or  $|B|, \phi, \gamma$ ) at a single height**
  - e.g., MERLIN or MEKSY Milne-Eddington technique assuming linear source function
  - RMO (“Integral”), JLS (“derivative”), etc methods also acceptable, but best to account for magneto-optical effects.
- No procedure (yet) solves the ambiguity as part of the inversion.

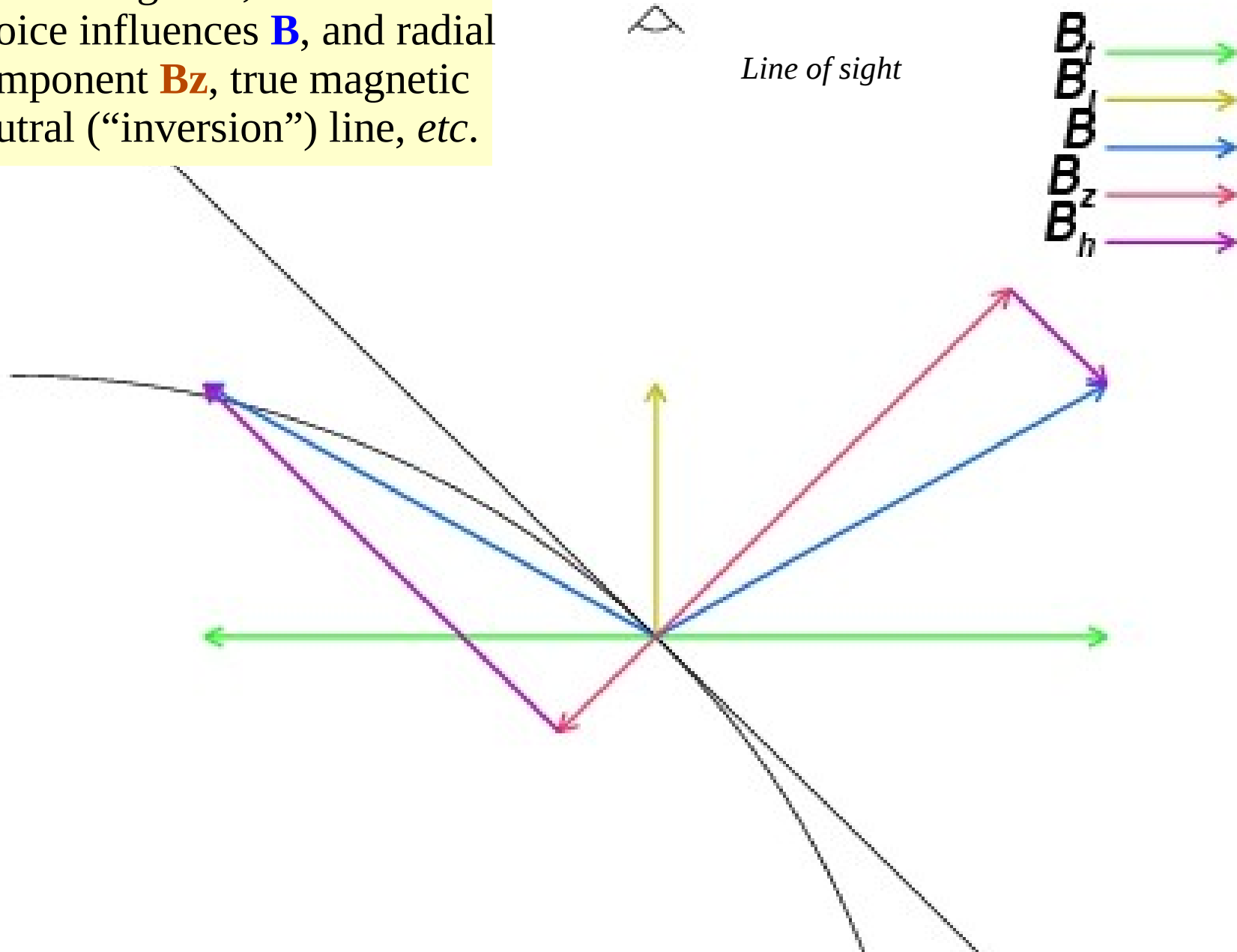


**Far left:  $B_{\parallel}$  of “Japan sunspot” at S10 W11 ( $\mu=0.98$ ), some false positive penumbral areas due to projection.**

**Left:  $B_z$ , radial field.**

## $B_{\text{trans}}$ direction must be chosen at each point

$B_t$  is ambiguous; direction choice influences  $B$ , and radial component  $B_z$ , true magnetic neutral (“inversion”) line, etc.



## ***NWRA's Automated Ambiguity Resolution***

- **Loosely based on the Minimum-Energy Approach:**

- Minimize the functional  $E = \sum \left( |J_z| + \nabla \cdot \vec{B} \right)$

- **$J_z$  requires derivatives in the horizontal, heliographic plane**

- $J_z$  employed rather than some approximation to  $J$ , to increase speed and reduce need for additional derivatives.

- **$\text{div}(\mathbf{B})$  requires derivatives in the *vertical* as well as horizontal direction.**

- The derivatives for  $\partial B_z / \partial z$  are computed from a potential field using the observed unambiguous line-of-sight field as the boundary.
  - Tests showed derivatives from the potential field were adequate if combined with a robust optimization

- **Now in Fortran**

- Accepts generic FITS, all Hinode L2 FITS, and formatted-array input
  - 512<sup>2</sup> magnetogram takes  $\approx 10$  minutes

## *NWRA's Automated Ambiguity Resolution, cont'd.*

- Global Optimization: Simulated Annealing is used to minimize the functional in strong-field areas.
  - Cooling schedule can be modified to best suit pipeline or targeted science.
- Weak-field areas solved by acute-angle to nearest-neighbor.
  - Propagate “correct” solution to areas dominated by noise.

## *Why “Minimum Energy” approach?*

- **Best-Performing automated algorithm when tested against a variety of modeled observational challenges:**

- highly-mixed potential/non-potential,
- off-disk-center constant twist
- off-disk-center constant twist with added photon noise
- effects of spatial resolution

See Metcalf et al 2006;  
Leka et al 2009 (in preparation)

- **Repeatable, objective.**

## Summary:

- Now available: a fast, Fortran code for solving the  $180^\circ$  azimuthal-angle ambiguity.
  - Based on the “minimum-energy” approach, best-performing in numerous objective model-based tests.
  - *All cases presented here ran in less than 10 minutes.*
  - Thus, “*Merit*” is high.
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- Available for use on L2 Hinode SOT/SP (and other **B** data) from:  
[www.cora.nwra.com/AMBIG/](http://www.cora.nwra.com/AMBIG/)
  - **Note:** still an “ $\alpha$ -version”, please try to make it fail so that we can fix it.