1	A case study on the far-field properties of propagating
2	tropospheric gravity waves
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ABSTRACT

Large-scale gravity waves were observed by barometers deployed as part of the USArray 8 Transportable Array on June 29, 2011 near two mesoscale convective systems in the Great 9 Plains region of the US. Simultaneously, AIRS satellite data indicated stratospheric gravity 10 waves propagating away from the location of active convection. Peak perturbation pressure 11 values associated with waves propagating outside of regions where there was precipitation 12 reached amplitudes close to 400 Pa at the surface. Here we investigate the origins of the waves 13 and their relationship to observed precipitation with a specialized model study. Simulations 14 with a 4-km resolution dry numerical model reproduce the propagation characteristics and 15 amplitudes of the observed waves with a high degree of quantitative similarity despite the 16 absence of any boundary layer processes, surface topography, or moist physics in the model. 17 The model is forced with a three-dimensional, time-dependent latent heating/cooling field 18 that mimics the latent heating inside the storms. The heating is derived from the network of 19 weather radar precipitation observations. This shows that deep, intense latent heat release 20 within the storms is the key forcing mechanism for the waves observed at ground level by the 21 USArray. Furthermore, the model simulations allow for a more detailed investigation of the 22 vertical structure and propagation characteristics of the waves. It is found that the strato-23 spheric and tropospheric waves are triggered by the same sources, but have different spectral 24 properties. Results also suggest that the propagating tropospheric waves may potentially 25 remotely interact with and enhance active storms. 26

²⁷ 1. Introduction

The Earthscope USArray Transportable Array (TA) is a network of approximately 400 28 seismo-acoustic stations deployed on a 70-km Cartesian grid covering an area of 2,000,000 29 km^2 in the continental United States (Busby et al. 2006). The network moved eastward 30 through station redeployments between 2004-2013, has since left the lower 48 states and is 31 being redeployed in Alaska. Although the array was originally designed for seismological 32 studies, in 2009 an atmospheric sensor package was deployed at TA sites along with the seis-33 mic sensors, recording pressure variations at the Earth's surface. Fig. 1 shows the locations 34 of operating stations equipped with these sensors for the years 2010-2013. 35

Propagating signals in surface pressure surrounding severe storms have been observed 36 with the TA, and were previously analyzed with a coherent detection method described 37 by De Groot-Hedlin et al. (2014). The large number of sensors placed on a nearly regular 38 Cartesian grid across a large region allows tracking of coherent signal propagation over long 39 distances, and their method was designed to minimize spatial aliasing problems. The results 40 showed that the typical 70-km spacing of the stations in the array permits the study of 41 coherent signals with periods longer than ~ 40 min and wavelengths longer than ~ 40 km. 42 These include a broad range of gravity waves with a wide range of propagation speeds. 43 De Groot-Hedlin et al. (2014) showed that the largest amplitude waves also had the longest 44 periods, and their analysis focused on signals in the 2-4 h band that displayed wavelengths 45 longer than the inter-station spacing. 46

Here we investigate the apparent relationship of the gravity wave surface pressure signals observed at ground level by the TA to severe storms using precipitation measurements from Next-Generation Radar (NEXRAD) weather radar stations and a specialized model previously shown to accurately simulate gravity waves in the far-field emanating from severe storms over the continental US. We will consider a broader band of 1-8 h that includes most gravity waves that are well-resolved by the array.

⁵³ Our study is an investigation into the origins of the observed waves, their propagation

and vertical structure, and their relationship to precipitation in a detailed case-study. The 54 selected case occurred during the night of June 28-29, 2011 over the central US when the 55 TA spanned 90-100 °W longitudes over the Great Plains west of the Mississippi. The case, 56 illustrated by radar mosaics in Fig. 2, includes two intense but relatively isolated storms: 57 One over the northeastern corner of Texas on the evening of June 28th and a second over the 58 Oklahoma Panhandle that intensified in the post-midnight hours of June 29th. These two 59 storms occurred near the eastern and western edges of the TA, respectively, and the relatively 60 isolated nature of the two storms makes this a good case for investigating the origins and 61 remote propagation of gravity waves observed in TA surface pressure measurements. 62

We use the modeling approach of Stephan and Alexander (2015) to simulate gravity 63 waves forced by realistically varying convective latent heating and cooling in an idealized 64 dry version of the Weather Research and Forecasting (WRF) model (Skamarock et al. 2008). 65 The heating/cooling field is three-dimensional and time-varying and derived directly from 66 the NEXRAD-observed precipitation using an algorithm described in Stephan and Alexander 67 (2015). The algorithm was trained on realistic simulations of severe storms with full-physics 68 WRF hindcasts, but the use of the idealized model with radar precipitation in the present 69 study permits direct comparisons to the spatial and temporal variations observed within the 70 TA. Such direct comparisons are not possible in full-physics WRF hindcasts because the 71 locations and timing of individual rain cells are never simulated accurately, yet these details 72 are crucial for accurate simulation of the gravity wave responses. 73

With this method, we will investigate the horizontal and vertical propagation characteristics of the gravity wave field, the wave amplitudes and relationship to precipitation. Previous studies have suggested a potential role for convectively-generated gravity waves in the organization of convective rain clouds (e.g. Mapes (1993); Yang and R. A. Houze (1995); Tulich et al. (2007)). Model studies have also suggested that convectively-generated gravity waves may initiate new convective cells in the far field (e.g. Shige and Satomura (2001), Fovell (2002)). While our dry model approach cannot directly investigate these feedbacks of gravity waves on precipitation, the model makes the normally invisible far-field gravity waves visible, permitting us to examine the realistically simulated gravity wave dynamics and their potential to influence low-level moisture convergence and precipitation. Also, through comparisons of the dry-modeled surface pressure anomalies to observed anomalies inside and outside of precipitating regions, we find evidence to support the hypothesis proposed in Bacmeister et al. (2012) that the mass of condensate in convective clouds can significantly influence surface pressure.

The paper is structured as follows: A summary of the weather situation during the 88 time of this case study will be given in Section 2.a. Method and numerical model will be 89 described in Section 2.b. We next examine the vertical structure of the simulated waves in 90 Section 2.c and use linear theory to relate the shape of the heating profiles to the propagation 91 characteristics of the waves. In Section 3 we compare the wave patterns and amplitudes of 92 simulated and observed waves to show that the model predicts the surface measurements with 93 good accuracy outside of precipitating regions. We further show that satellite observations 94 of waves in the stratosphere above the storm are consistent with both the model predictions 95 and observations at ground level. Section 4 examines the potential for the far-field gravity 96 wave response associated with these storm events to intensify remote convection. Section 5 97 is a summary and conclusion. 98

⁹⁹ 2. Numerical simulations

100 a. Weather conditions

During the time period of this case study, June 28-29, 2011, the large-scale synoptic pattern over North America at 500 hPa was dominated by a broad ridge centered over New Mexico/Texas that extended from the west coast to Florida. This high-pressure system caused record-breaking high temperatures in the southern US. At 12:00 UTC on June 28 a cold front extended from southeastern New Mexico to Tennessee. A series of severe storms

developed along this front and moved southeastward over the course of the following 12 106 hours. The storm marked by an arrow in Fig. 2 over South-East Oklahoma was a remnant 107 of these storms. After 01:00 UTC this system decayed. By 23:30 UTC on June 28 the cold 108 front had turned into a stationary front that extended from the Oklahoma Panhandle along 109 the Texas-Oklahoma boarder into northern Arkansas. This front separated hot air with 110 surface temperatures exceeding 37°C in Texas from relatively cooler air to the north with 111 surface temperatures of about 30° C, and a new storm system was developing on the southern 112 side of the front. The storm was located on the western end of the Oklahoma Panhandle 113 and extended into Colorado and New Mexico. The front propagated northward and by 14:00 114 UTC on June 29 was located north of Oklahoma. Meanwhile the Panhandle storm formed 115 into a well organized squall line, which is clearly visible at 01:00 UTC in Fig. 2, and it moved 116 eastward into Central Oklahoma. (See Fig. 2 at 7:30 UTC.) After 08:00 UTC this storm 117 started to decay as well. 118

119 b. Model and method

This study uses the modeling approach described in Stephan and Alexander (2015), 120 where a nonlinear idealized dry version of the WRF model is forced with 4-km resolution 121 latent heating/cooling derived from NEXRAD precipitation observations. The model does 122 not include moist processes, a boundary layer, nor topography. A vertical heating/cooling 123 profile is assigned to each grid point where the local precipitation rate exceeds 1 mm/10124 min and is updated every 10 min. See Stephan and Alexander (2015) for details on the 125 algorithm for generating the heating profiles. For several case studies it was shown that 126 this model produces an excellent quantitative comparison to waves in the stratosphere that 127 were observed by satellite. However, until now the realism of the simulated waves in the 128 troposphere has not been validated. 129

Fig. 3 shows the 2000 km \times 2000 km model domain in gold and the locations of individual NEXRAD radar stations that are used to derive a 4 km \times 4 km 10 min mosaic of precipitation. We obtain the Storm Total Rainfall Accumulation Product (STP, OFCM (2006)) for individual NEXRAD stations, which provides radar-estimated rainfall accumulations within 230 km of the radar in polar coordinates with a resolution of 2 km \times 1°. Data from the individual stations are then interpolated in space and time to obtain Cartesian gridded maps.

The model run is initialized at 20:00 UTC on 28 June 2011 with one-dimensional horizontal-137 wind and potential temperature profiles, shown in Fig. 4. These are derived by averaging 138 reanalyzed winds and temperatures from the Modern-Era Retrospective analysis for Re-139 search and Applications (MERRA, Rienecker et al. (2011)) over 24 h in the region within 140 the dashed rectangle shown in Fig. 3. This area marks the region of strongest storm activity 141 during the simulated period 20:00 UTC on 28 June, 2011 to 20:00 UTC on 29 June, 2011. 142 The model includes 99 evenly spaced vertical levels extending from the surface to 24 km (30) 143 hPa) with the upper 5 km consisting of a damping layer to prevent wave reflection. 144

Fig. 5 shows simulated pressure perturbations at 500 m above the surface at 2, 6 and 145 10 UTC. Red colors mark rain cells that exceed the convective threshold of 1 mm/10 min, 146 i.e. regions where the heating field in the idealized model is nonzero. At 02:00 UTC both 147 of the storm centers marked by arrows in the left panel of Fig. 2 are visible. The storm 148 centered at $\sim 95^{\circ}$ W is triggering strong westward propagating pressure waves with peak to 149 peak amplitudes on the order of 300 Pa. A negative perturbation pressure wave is followed 150 by a more slowly moving positive wave. The positive perturbation pressure wave reaches 151 the other storm center located at $\sim 100^{\circ}$ W around 05:30 UTC. This second storm is also 152 triggering waves, which are clearly visible at the surface at 10:00 UTC. 153

From these maps and Fig. 2 it is apparent that most of the precipitation, and therefore waves, in the model domain and the surrounding region of the US are associated with the two well-confined storm systems. However, at 02:00 UTC and 10:00 UTC some isolated cells exist in the southeast corner of the model domain. While these wave-generating cells are included in the model, other cells that lie outside of the model domain are not. When comparing to observations in Section 3 it should be taken into account that waves can propagate long distances and that some of the wave signals in the observations may be attributed to sources that lie outside of the simulated area.

¹⁶² c. Wave vertical structure and propagation characteristics

As mentioned in Section 1, the TA is a very useful observational network for studying the occurrence frequencies and horizontal propagation characteristics of gravity waves at the surface. The WRF simulation in addition is able to reveal the vertical structure of these waves, which is required for explaining their propagation characteristics and for assessing the impact such waves may have on the atmosphere hundreds of kilometers away from their origin.

Fig. 6 is a zonal cross section at 34°N and 00:40 UTC showing the vertical structure of 169 small-scale propagating waves to the west of an active center of convection. The line to the 170 left of each panel shows the shape of the mean heating/cooling profile inside the convective 171 region as derived by the heating algorithm from observed precipitation, and the thin black 172 line marks a value of zero. From the top panel of Fig. 6, which shows vertical velocity, we 173 observe that the characteristic depth of the waves in the troposphere corresponds to the 174 depth of the heating. Also evident are waves propagating into the stratosphere with shorter 175 vertical scales. For medium frequency gravity waves, the group velocity vector is along lines 176 of constant phase and the ratio of the intrinsic vertical group velocity to the horizontal group 177 velocity can be expressed as 178

$$|\hat{c}_{gz}/\hat{c}_{gh}| = |k_h/m| = |k_h \frac{\hat{c}_h}{N_{BV}}| = |\frac{\hat{\omega}}{N_{BV}}|, \qquad (1)$$

where k_h is the horizontal wave number, \hat{c}_h the intrinsic horizontal phase speed, m the vertical wave number and $\hat{\omega}$ the intrinsic frequency (Fritts and Alexander 2003). Since this quantity is inversely proportional to the buoyancy frequency N_{BV} , which in the stratosphere has approximately double its tropospheric value, waves get refracted to shorter vertical ¹⁸³ wavelength as they cross the tropopause, as evident in Fig. 6.

The bottom panel of Fig. 6 shows the corresponding perturbation pressure. Note that 184 the anomalies are all positive because of the focus here on a small region that lies within 185 the positive phase of the larger scale wave described in Fig. 5. Amplitudes are largest at 186 the surface and decay linearly with altitude. In reality the Earth's surface in the area of 187 interest is not flat but its elevation varies between 0.0-1.2 km above sea level. Given that 188 the large-scale variations in pressure are on the order of several hundred Pa (see Fig. 5) we 189 will neglect topography when comparing to the surface observations in Section 3, and focus 190 on the model level at 500 m. 191

The vertical structure of the vertical velocity field displays some complexity. From linear theory it is expected that several wave modes are generated by the typical heating profiles in the model. Fig. 7 shows the decomposition of a heating profile H(z) associated with a strong rain rate (thick black line in the right panel) into its first 10 (left panel) and first 3 (middle panel) Fourier components. The decomposition is given by

$$H(z) = \sum_{n=1}^{n=N} A_n \sin \frac{\pi n z}{D}.$$
(2)

Here, $D \approx 11$ km denotes the depth of the heating, which we define as the vertical distance between the bottom of the cooling layer and the top of the heating region. The heating profile H(z) is computed for a rain rate of 14 mm/10min, which corresponds to the 99th percentile of 4 km × 4 km 10-min rain rates seen this study. The colored lines in Fig. 7 are the respective sums of the individual modes and are also shown in the right panel for comparison with the original profile.

As has been shown in Nicholls et al. (1991), linear theory predicts that the horizontal phase speed for a pure sine mode is given by

$$c_h = \frac{D}{n} \frac{N_{BV}}{\pi}.$$
(3)

The mean buoyancy frequency $N_{BV} = 0.012 \text{ s}^{-1}$ in the heating/cooling region is computed from the initialization profile of dry potential temperature shown in Fig. 4. Table 1 shows the theoretical phase speeds and the relative contributions $|A_n/A_0|$ for the first ten Fourier modes. A_0 is the maximum heating rate of H(z). The phase speed values are not very sensitive to the rain rate that was assumed in computing H(z). For a 50% smaller rain rate phase speeds remain within 5% of those shown in Table 1.

Fig. 8 shows normalized absolute momentum flux spectra, given by

$$F(\kappa, f) = \sqrt{(\hat{u}\hat{w}^*)^2 + (\hat{v}\hat{w}^*)^2}$$
(4)

at 3 km (left panel) and 17 km (right panel) as a function of wavenumber and frequency. 212 These spectra are computed from perturbation wind velocities using a three-dimensional 213 Fourier analysis. Details of the computation are described in Stephan and Alexander (2014). 214 Lines of constant phase speed labeled in units of m/s are shown in white. Comparing to 215 Table 1 we find that linear theory successfully predicts the main characteristics of these 216 spectra. Prominent lobes appear near the predicted top four (n = 1, 2, 3, 4) mode speeds 217 of 40, 20, 15 and 10 m/s. The n = 1 mode is more pronounced in the stratosphere at 218 17 km compared to the 3 km level and the slowest n > 5 modes are more prominent in 219 the troposphere. Equation 1 predicts that for a given horizontal wavenumber k_h waves with 220 larger horizontal phase speeds \hat{c}_h escape into the stratosphere more quickly. This is consistent 221 with the relatively larger abundance of slow (fast) waves in the troposphere (stratosphere). 222

223 3. Comparisons with observations

This study uses data from barometric pressure sensors in the atmospheric sensor package deployed at each site of the TA. These instruments measure ambient pressure with an accuracy of 0.2 Pa, with the data digitized at 1 Hz. For further details see De Groot-Hedlin et al. (2014).

Fig. 9 shows model perturbation pressure in units of Pa sampled at locations of TA installations and the corresponding TA recorded observations at 2-h intervals. A 1-8 h bandpass filter has been applied to both data sets. Time stamps in UTC are embedded in each panel.

Comparing to Fig. 5 at 02:00 UTC, we recognize the prominent negative perturbation wave 231 that is followed by a strong positive perturbation. There is good agreement between the 232 simulation and observations in terms of amplitude, location and wavelength of this pattern. 233 We see the waves propagating westward at later times and leaving the region of the TA. In 234 the 06:00 UTC panel a positive perturbation located above the Oklahoma Panhandle storm 235 starts near 37°N at the western side of the TA region and then propagates southeastward. 236 There is again good agreement in amplitudes and size of this feature between model and 237 observations. At 12:00 UTC storm and wave activity have mostly calmed down, but pres-238 sure perturbations on the order of 30 Pa remain. The model predicts the spatial extent and 239 magnitudes of these residual perturbations very well. 240

To better see the realistic representation of the timing, speed and amplitudes of the waves 241 in the model, Fig. 10 shows time series from the simulations (panel a) and TA data (panel 242 b). The TA data have been de-meaned and bandpass filtered from 1-8 h and the model 243 domain-mean pressure has been subtracted from the simulated data at each time. All lines 244 are normalized such that 1° in longitude corresponds to a pressure perturbation of 300 Pa. 245 There are several differences in the details of the waves but the overall agreement between 246 model and observations for the most intense wave trains is good. Their timing, propagation 247 speed and dissipation are simulated rather accurately. Red colors mark regions where rain 248 exceeds 1 mm/10 min. There is indication from this comparison that perturbations may be 249 underestimated in the model in regions where there was precipitation. 250

Fig. 11 compares the simulated (solid histograms) and observed (dashed histograms) absolute perturbation pressure amplitudes of Fig. 10 close to convective regions (red) and to areas in the far-field (blue), defined here as regions that are separated by at least 0.75° of latitude/longitude from locations where rain rates greater than 1 mm/10 min are observed. Data are normalized by the total number of grid points in the far-field and grid points in the vicinity of convection, respectively. The relative occurrence frequency of large perturbation pressure amplitudes is much greater for regions in the vicinity of convection, even though

substantial amplitudes greater than 200 Pa are reached in the observed far-field wave field. 258 The potential for these waves to interact with or trigger remote convection will be discussed 259 further in Section 4. Furthermore we see that the model underestimates the amplitudes 260 of waves in regions where there was precipitation, which we label as convectively coupled 261 waves. We hypothesize that this difference between model and observation is due to the fact 262 that the model does not include moist processes. Bacmeister et al. (2012) show that the 263 mass of condensate in convective clouds can significantly influence surface pressure, leading 264 to corrections on the order of ~ 100 Pa. 265

The vertical velocity field in Fig. 6 and the momentum flux spectrum at 17 km in Fig. 8 266 indicate that some of the wave energy also propagates upward into the stratosphere. The 267 Atmospheric Infrared Sounder (AIRS) aboard NASA's Aqua satellite is a hyper-spectral 268 imager, and can observe gravity wave signals in the stratosphere at 4.3 micron as well as cloud 269 top brightness temperatures at 8.1 micron Hoffmann and Alexander (2010). Low 8.1 micron 270 brightness temperatures observed by AIRS when the satellite passed over 36°N, 98°W at 271 08:05 UTC on June 29 indicate a mesoscale convective system with convection overshooting 272 the tropopause (left panel of Fig. 12). This storm system is marked by the arrow in the right 273 panel of Fig. 2. Simultaneous 4.3 micron brightness temperature perturbations indicate 274 stratospheric gravity waves propagating to the east from this location. 275

Eastward propagating waves were seen at the surface as well, see Fig. 5 at 10:00 UTC and the 35°N-36°N panel of Fig. 10. Fig. 13 is a zonal cross section at 07:00 UTC at 35.5°N, showing the vertical velocity field in shades of gray and the heating/cooling region in purple. It shows the deep tropospheric waves that can be seen at the surface and waves propagating eastward into the stratosphere. The stratospheric waves have a horizontal wavelength of about one degree longitude, which is consistent with the horizontal wave length scales observed by the satellite.

²⁸³ 4. Potential wave impacts on convection

In the previous sections we have seen that the model is capable of producing realistic gravity waves in the troposphere and above. Unlike surface or satellite observations the simulations contain information about the vertical structure of these waves and give us a more complete picture of their properties. We will now investigate the potential for these waves to impact active convection.

Fig. 14 displays hourly maps of vertical displacement at 850 hPa calculated as

$$\Delta z = -\Delta \theta \left(\frac{\partial \theta}{\partial z}\right)^{-1},\tag{5}$$

where $\Delta \theta$ is the potential temperature perturbation at 850 hPa and $\partial \theta / \partial z$ is the vertical 290 gradient of potential temperature, obtained from the initialization profile Fig. 4. Each panel 291 shows the 2000 km \times 2000 km WRF model domain, and time in UTC is given in the bottom 292 left of each panel. Precipitating regions as determined by the radar observations are again 293 marked in red. The blue box encloses the Oklahoma Panhandle storm and numbers above 294 each box show the accumulated hourly areal mean precipitation in mm for the area of the 295 box. To better resolve the temporal evolution of precipitation inside the box the plot at 296 the top of Fig. 14 shows the corresponding mean 10 min rain rates between 00:00 and 08:00 297 UTC. 298

We observe a westward propagating wave consisting of a wide-spread area with negative 299 displacement followed by a well-defined positive-displacement. These waves are triggered 300 by the storm located in the center of the domain at 01:00 UTC and their signature was 301 also apparent in the pressure perturbations shown in Fig. 5. An approximate doubling of 302 the precipitation rate occurs as the positive phase of the propagating wave encounters the 303 storm active inside the box. This information is insufficient to establish a causal relationship 304 between the wave and the strengthening of the storm but it is consistent with the hypothesis 305 that the gravity wave vertical displacements on the order of several hundred meters may 306 alternately interfere with active convection and enhance it. 307

Fig. 15 is a Hovmoeller diagram of vertical displacement at 34°N showing the region 308 104.1°W to 94.4°W. Precipitation is shown in red. The black dashed (dotted) lines mark 309 constant propagation speeds of 40 (20) m/s relative to the mean zonal wind of 3 m/s in the 310 heating region. We can see that the negative displacement pressure wave has a faster prop-311 agation speed than the positive displacement wave. The positive wave travels at a velocity 312 close to the n = 2 mode, (see Table 1). The positive perturbation remains visible at the 313 surface at distances far away from its origin, as opposed to the negative wave which appears 314 to be more dispersive. This is consistent with the horizontal maps shown in Fig. 14. The 315 discussion in the last paragraph of Section 2.c suggests further that the negative displace-316 ment wave would propagate upward more quickly than the positive wave due to a larger 317 horizontal phase speed, higher wavenumber, and therefore faster vertical energy propagation 318 according to Equ. 1. This effect may contribute to the more rapid attenuation of the negative 319 displacement signal at the surface. 320

The linear response to gravity waves from a radially symmetric heating profile on isen-321 tropic displacements near the surface has been calculated in Mapes (1993). They assumed 322 a heating profile consisting of two modes, one with a vertical wavelength of twice the depth 323 of the heating (n=1) and one with a wavelength equal to the depth of the heating (n=2). 324 In agreement with our nonlinear simulations and the TA observations they report that 3 h 325 after a heating pulse, low-level isentropes are lifted at a distance of about 250 km from the 326 heating while the faster-propagating n = 1 results in subsidence at distance of about 500 327 km, see their Fig. 4b. The good agreement with theory and observations suggests that the 328 findings of this study may apply more generally, not only to the specific storm case examined 329 here. 330

331 5. Summary

In this case study we simulated gravity waves generated by latent heating in storms over 332 the central US. Model and observations show that these waves are associated with surface 333 pressure signals that propagate distances longer than several hundred km and commonly 334 exceed amplitudes of 100 Pa. In our model, described previously in Stephan and Alexan-335 der (2015), waves are forced by a temporally and spatially varying heating/cooling field 336 that is derived directly from radar-observed precipitation. This approach permits a direct 337 comparison to surface pressure variations measured by barometers in the USArray Trans-338 portable Array and we find wave amplitudes agree well outside of regions where there was 339 precipitation. The model renders the 3-dimensional far-field wave structure visible, which 340 normally is unknown because measurements tend to be limited to the surface or provide 341 vertical information at individual points only. 342

We analyzed wave propagation characteristics across the full vertical extent of the tro-343 posphere and found that linear theory can successfully predict the propagation speed of the 344 simulated waves from the shape of the vertical heating profiles. From Fig. 8, slower waves 345 with speeds < 5 m/s are relatively more prominent at the surface, and faster waves > 20346 m/s are relatively more prominent near the tropopause, which can be understood as a con-347 sequence of their respective slow and fast vertical group velocities. Waves with intermediate 348 speeds of 5-20 m/s are common at all levels. Similar wave signatures as those seen in the 349 model were also observed in an overpass of the AIRS satellite instrument, indicating that 350 waves measured at the surface and waves observed in the stratosphere are originating from 351 common storm sources. 352

Vertical air parcel displacements at 850 hPa caused by waves propagating into regions that are far away from active convection exceed several hundred meters. In particular, we found evidence that the lifting phase of a 20 m/s propagating wave could be potentially responsible for an observed intensification of a separate developing storm. The interaction of the propagating storm with the convection occurred several hundred kilometers away from the origin of the wave and roughly 5 h after the wave was triggered.

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REFERENCES

- Bacmeister, J. T., P. H. Lauritzen, A. Dai, and J. E. Truesdale, 2012: Assessing possible
 dynamical effects of condensate in high resolution climate simulations. *Geophys. Res. Lett.*,
- **375 39**, L04 806, doi:10.1029/2011GL050533.
- ³⁷⁶ Busby, R., F. Vernon, R. Newman, and L. Astiz, 2006: Eos Trans. AGU 87 (52). Fall Meet.
 ³⁷⁷ Suppl., Abstract U41B-0820. Earth-Scopes USArray: Advancing eastward.
- ³⁷⁸ De Groot-Hedlin, C., M. Hedlin, and K. Walker, 2014: Detection of gravity waves across the
- USArray: A case study. *Earth and Planetary Sci. Lett.*, 402, 346–352, doi:10.1016/j.epsl.
 2013.06.042.
- Fovell, R. G., 2002: Upstream influence of numerically simulated squall-line storms. Q. J. *R. Meteorol. Soc.*, **128**, 893–912.
- Fritts, D. C. and M. J. Alexander, 2003: Gravity wave dynamics and effects in the middle
 atmosphere. *Rev. Geophys.*, 41, 1003, doi:10.1029/2001RG000106.
- Hoffmann, L. and M. J. Alexander, 2010: Occurrence frequency of convective gravity waves
 during the North American thunderstorm season. J. Geophys. Res., 115, doi:10.1029/
 2010JD014401.
- ³⁸⁸ Mapes, B. E., 1993: Gregarious tropical convection. J. Atmos. Sci., 50, 2026–2037.
- Nicholls, M. E., R. A. Pielke, and W. R. Cotton, 1991: Thermally forced gravity waves
 in an atmosphere at rest. J. Atmos. Sci., 48, 1869–1884, doi:http://dx.doi.org/10.1175/
 1520-0469(1991)048(1869:TFGWIA)2.0.CO;2.
- ³⁹² OFCM, 2006: Federal meteorological handbook No. 11 part c. OFCM Tech. Rep. FCM ³⁹³ H11C-2006.

- Rienecker, M. M., et al., 2011: MERRA: NASA's Modern-Era Retrospective Analysis for
 Research and Applications. J. Climate, 24, 3624–3648, doi:10.1175/JCLI-D-11-00015.1.
- Shige, S. and T. Satomura, 2001: Westward generation of eastward-moving tropical convective bands in TOGA COARE. J. Atmos. Sci., 58, 3724–3740, doi:http://dx.doi.org/10.
 1175/1520-0469(2001)058(3724:WGOEMT)2.0.CO;2.
- ³⁹⁹ Skamarock, W., J. B. Klemp, J. Dudhia, et al., 2008: A description of the Advanced Research
 ⁴⁰⁰ WRF Version 3. NCAR Technical Note NCAR/TN-475+STR. doi:10.5065/D68S4MVH.
- Stephan, C. C. and M. J. Alexander, 2014: Summer season squall line simulations: Sensitivity of gravity waves to physics parameterization and implications for their parameterization
 in global climate models. J. Atmos. Sci., 71, 3376–3391, doi:10.1175/JAS-D-13-0380.1.
- Stephan, C. C. and M. J. Alexander, 2015: Realistic simulations of atmospheric gravity
 waves over the Continental U.S. using precipitation radar data. J. Adv. Model. Earth
 Syst., 07, 823–835, doi:10.1002/2014MS000396.
- Tulich, S. N., D. A. Randall, and B. E. Mapes, 2007: Vertical-mode and cloud decomposition of large-scale convectively coupled gravity waves in a two-dimensional cloud-resolving
 model. J. Atmos. Sci., 64, 1210–1229, doi:10.1175/JAS3884.1.
- Yang, M.-J. and J. R. A. Houze, 1995: Multicell squall-line structure as a manifestation of vertically trapped gravity waves. *Mon. Wea. Rev.*, **123**, 641–660, doi:10.1175/
 1520-0493(1995)123(0641:MSLSAA)2.0.CO;2.

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⁴¹⁴ 1 Theoretical phase speeds c, from Equ. 3, and the relative contribution $|A_n/A_0|$, ⁴¹⁵ from Equ. 2, for the first ten Fourier modes. Please refer the text for further ⁴¹⁶ explanation.

TABLE 1. Theoretical phase speeds c, from Equ. 3, and the relative contribution $|A_n/A_0|$, from Equ. 2, for the first ten Fourier modes. Please refer the text for further explanation.

n	c [m/s]	$ A_n/A_0 $
1	42.6	86.3
2	21.3	30.3
3	14.2	12.2
4	10.6	10.6
5	8.5	4.0
6	7.1	4.7
7	6.1	1.4
8	5.3	2.0
9	4.7	0.2
10	4.3	0.5

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Il Simulated absolute perturbation pressure amplitudes in the vicinity of precipitating regions (red), defined as areas separated by less than 0.75° of latitude/longitude from locations where rain rates greater than 1 mm/10 min are observed and far-field areas (blue). Simulated data are shown as solid histograms and observed data as dashed histograms. All data are normalized by the total number of grid points that lie in the far-field and in the vicinity of convection, respectively.

- 8.1 micron brightness temperatures (left) and 4.3 micron brightness tempera-12470 ture perturbations (right) observed by AIRS at 08:05 UTC on June 29 indicate 471 a mesoscale convective system with convection overshooting the troppause 472 and eastward propagating gravity waves, respectively. The images are com-473 puted using the method described in Hoffmann and Alexander (2010). 474 Zonal cross section at 07:00 UTC at 35.5°N, showing vertical velocities (shades 13475 of gray) and the heating/cooling region (purple) at contour intervals of 0.003476
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14Hourly maps of vertical displacement at 850 hPa computed from simulated 478 potential temperature perturbations. Time in hours UTC is indicated in 479 the bottom left of each panel. Red areas mark active convection (rain rates 480 exceeding 1 mm/10 min for some time during the hour). The areal-mean 481 precipitation rate in mm/hour inside the box is shown above the blue box 482 inside each panel. The graph at the top of the figure shows the temporal 483 evolution of areal-mean 10 min precipitation inside the box between 00:00 484 and 08:00 UTC. 485

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Hovmöller diagram of 850 hPa vertical displacement at 34°N showing the
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mm/10 min).



FIG. 1. Deployment history of operating Transportable Array stations equipped with MEMS (Micro Electro-Mechanical System) pressure sensors for the years 2010-2013.



FIG. 2. National NEXRAD 1-km mosaic of radar reflectivity, available at www2.mmm.ucar.edu/imagearchive/. Arrows point to the storms of interest within this study.



FIG. 3. Model domain measuring 2000 km \times 2000 km (gold) and NEXRAD radar stations that are used for deriving a 4 km \times 4 km 10 min precipitation mosaic. The four-letter identification code indicates the location and the circles the 230 km radius of individual stations. The simulation is initialized using MERRA vertical profiles averaged inside the dashed black box.



FIG. 4. Initialization profiles of potential temperature and horizontal winds computed from 24-h mean MERRA profiles. MERRA grid points inside the black dashed box shown in Fig. 3 were averaged.



FIG. 5. Maps of simulated perturbation pressure, defined as the deviation from the domain mean pressure at each time, at 500 m altitude. Red areas mark regions that exceed the convective threshold of 1 mm/10 min, i.e. regions where a heating/cooling field is turned on in the simulation.



FIG. 6. Zonal cross sections of vertical velocities (top) and perturbation pressure (bottom) at 34°N and 00:40 UTC to the west of active convection. The origin of the x-axis is located at 96.2°W. The color scale for the top panel is saturated at \pm 1.5 m/s to emphasize the far-field waves, but vertical velocity values close to the heat source range from -2.3 m/s to +3.0 m/s. The shape of the mean heating/cooling profile inside the convective region is shown to the left of each panel.



FIG. 7. Decomposition of the heating profile associated with the 99th percentile rain rate. The full heating profile is shown in the right panel (thick black line). The sums of the first 10 (left panel) and first 3 (middle panel) Fourier components are colored lines. For details on the computation, please refer to the text.



FIG. 8. Normalized absolute momentum flux spectra at 3 km (left panel) and 17 km (right panel) as a function of wavenumber and frequency. Lines of constant phase speed in units of m/s are shown in white.



FIG. 9. Model perturbation pressure in units of Pa sampled at locations of TA installations and the corresponding TA recorded observations at 2-h intervals. A 1-8 h bandpass filter has been applied to both data sets. Time in UTC is shown at the bottom inside each panel.



FIG. 10. Times series of model predictions and recorded data at locations of stations in the TA. We have arranged all model predictions in a set of 8 sections in a), with observations in b). Each panel contains recordings (or model predictions) from all stations that were located in a narrow east-west corridor - with the latitude limits given in the figure captions, and with the zero-anomaly location of each trace along the x-axis being determined by the stations longitude. Amplitudes are normalized such that 300 Pa correspond to 1° of longitude. The observed time series were bandpass filtered from 1-8 h. For simulated data the domain-mean pressure at each time has been removed. Regions of active convection are marked in red (rain rates exceeding a threshold of 1 mm/10 min).



FIG. 11. Simulated absolute perturbation pressure amplitudes in the vicinity of precipitating regions (red), defined as areas separated by less than 0.75° of latitude/longitude from locations where rain rates greater than 1 mm/10 min are observed and far-field areas (blue). Simulated data are shown as solid histograms and observed data as dashed histograms. All data are normalized by the total number of grid points that lie in the far-field and in the vicinity of convection, respectively.



FIG. 12. 8.1 micron brightness temperatures (left) and 4.3 micron brightness temperature perturbations (right) observed by AIRS at 08:05 UTC on June 29 indicate a mesoscale convective system with convection overshooting the tropopause and eastward propagating gravity waves, respectively. The images are computed using the method described in Hoffmann and Alexander (2010).



FIG. 13. Zonal cross section at 07:00 UTC at 35.5° N, showing vertical velocities (shades of gray) and the heating/cooling region (purple) at contour intervals of 0.003 K/s.



FIG. 14. Hourly maps of vertical displacement at 850 hPa computed from simulated potential temperature perturbations. Time in hours UTC is indicated in the bottom left of each panel. Red areas mark active convection (rain rates exceeding 1 mm/10 min for some time during the hour). The areal-mean precipitation rate in mm/hour inside the box is shown above the blue box inside each panel. The graph at the top of the figure shows the temporal evolution of areal-mean 10 min precipitation inside the box between 00:00 and 08:00 UTC.



FIG. 15. Hovmöller diagram of 850 hPa vertical displacement at 34° N showing the region 104.1° W to 94.4° W. Black dashed (dotted) lines mark constant propagation speeds of 40 (20) m/s relative to the mean zonal wind of 3 m/s in the heating region. Precipitating regions are shown in red (rain rates exceeding 1 mm/10 min).