- Gravity Wave Activity during Stratospheric Sudden
- Warmings in the 2007/08 Northern Hemisphere Winter

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X - 2 WANG AND ALEXANDER: GRAVITY WAVE ACTIVITY DURING SSWS We use temperature retrievals from the Constellation Observ-Abstract. 8 ing System for Meteorology, Ionosphere and Climate (COSMIC)/Formosa Satellite Mission 3 (FORMOSAT-3) and Challenging Minisatellite Payload 10 (CHAMP) Global Positioning Satellite (GPS) radio occultation profiles and 11 independent temperature retrievals from the EOS satellite High Resolution 12 Dynamics Limb Sounder (HIRDLS) and Sounding of the Atmosphere using 13 Broadband Emission Radiometry (SABER) aboard the TIMED satellite to 14 investigate stratospheric sudden warming (SSW) events and the accompa-15 nying gravity wave (GW) temperature amplitudes in the 2007/08 Northern 16 Hemisphere winter. We identify four SSW events (including a major one) oc-17 curring from late January to late February in 2008. We detect enhanced GW 18 amplitudes in the stratosphere and subdued GW amplitudes in the lower meso-19 sphere during the warming events. The timing of GW enhancement/suppression 20 and warming/cooling events was generally close (within a couple days). We 21 also find that stratospheric GW amplitudes were generally larger at the po-22 lar vortex edge, and smaller in the vortex core and outside of the vortex, and 23 stratospheric GW amplitudes were generally small over the north Pacific. Us-24 ing a simplified GW dispersion relation and a GW ray-tracing experiment, 25 we demonstrate that the enhanced GW amplitudes in the stratosphere dur-26 ing SSWs could be explained largely by GW propagation considerations. The 27 existence of GW critical levels (the level at which the background wind is 28 the same as the GW phase speed) near the stratopause during SSWs would 29

<sup>30</sup> block propagation of GWs into the mesosphere and thus could lead to the
<sup>31</sup> observed subdued GW activity in the lower mesosphere.

Since this is the first study to analyze the COSMIC and CHAMP GPS temperature retrievals up to 60 km in altitude, we compare the GPS analysis with those from HIRDLS and SABER measurements. We find that the temporal variability of zonal mean temperatures derived from the GPS data is reasonable up to  $\sim$  60 km in altitude, but the GPS data were less sensitive to SSWs than HIRDLS and SABER. GW analysis from GPS is consistent with HIRDLS up to  $\sim$  35 km in altitude but it seems that the small-scale

<sup>39</sup> variability at higher altitudes revealed in the GPS data is questionable.

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## 1. Introduction

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Stratospheric sudden warmings (SSWs) are large-scale transient events in the winter 40 polar middle atmosphere. They affect the middle atmosphere structure and general circu-41 lation profoundly [Andrews et al., 1987] and could also have significant impacts on weather 42 in the troposphere [Baldwin and Dunkerton, 2001]. During an SSW event, the zonal mean 43 temperatures in the polar middle stratosphere increase by several tens of Kelvins within 44 a few days. The warming is accompanied by the weakening of the polar vortex and west-45 erly winds (and even complete breakdown of the polar vortex and reversal of zonal mean 46 zonal winds in the case of a major event). SSWs are also observed to be accompanied by 47 significant coolings in the mesosphere.

SSWs are the most dramatic example of dynamical coupling of the lower and middle 49 atmosphere. They are commonly believed to be caused by the interaction of wavenumber 50 1 or 2 Rossby waves originating from the lower atmosphere with the mean flow [Matsuno, 51 1971]. When those westward propagating waves enter the polar stratosphere, they exert 52 a westward acceleration (thus weakening or even reversing the normally westerly flow) 53 through wave dissipation or wave transience (i.e., the Eliassen-Palm flux divergence). 54 This westward zonal force is partly offset by the Coriolis force and induces a poleward 55 residual circulation causing sinking motion below and poleward of the forcing region. The 56 adiabatic temperature changes give rise to the warming observed in the polar stratosphere. 57 Due to mass balance, the poleward residual circulation also causes adiabatic ascent above 58 and poleward the forcing region, thus explaining the accompanying mesospheric cooling 59 [Matsuno and Nakamura, 1979]. 60

Due to the dramatic change of the background atmosphere within a very short period 61 of time, SSWs affect gravity wave (GW) propagation and transmission in the middle 62 atmosphere profoundly. For example, orographically generated stationary GWs would 63 be absorbed by the mean atmosphere as they approached the zero mean zonal wind 64 level in the course of a SSW. Such interaction of GWs and winds during SSWs would 65 have significant impacts on the structure and general circulation in the mesosphere as 66 the resulting reduction in GW drag and diffusion would imply a reduced amplitude for 67 mean meridional circulation which is induced by GW breaking. The reduced meridional 68 circulation during SSWs implies a colder winter polar mesosphere which is normally much 69 warmer than radiative equilibrium. As argued by *Holton* [1983], this mechanism explains 70 better the observed broad depth of mesospheric coolings than the secondary meridional 71 circulation mechanism proposed by Matsuno and Nakamura [1979] mentioned above. The 72 modified GW properties during SSWs could also affect the mean atmosphere below the 73 middle stratosphere via the downward control principal [Haynes et al., 1991; Garcia and 74 *Boville*, 1994]. 75

There have been a few observational studies to examine GW activity during SSWs 76 in the past few decades. Duck et al. [1998] examined the relationship between GWs 77 and SSWs using lidar temperature measurements in the stratosphere over Eureka (80°N, 78 86°W). They detected increased GW activity in the polar vortex jet during the warming. 79 Ratnam et al. [2004] examined GW activity during the unprecedented major SSW in the 80 Southern Hemisphere in 2002 using the CHAMP GPS temperature profiles. They found 81 that GW potential energies in the stratosphere below 30 km increased three-fold during 82 the event. Wang et al. [2006] analyzed rocket soundings obtained from the MaCWAVE 83

winter campaign and found clear evidence of topographic GWs approaching their critical levels during an SSW event. *Dowdy et al.* [2007] investigated the dynamical response of the polar mesosphere and lower thermosphere to SSWs using MF radar horizontal wind data at two Antarctic and two Arctic sites. They found that SSWs had a variable effect on mesospheric GW activity, depending on factors such as location, GW frequency, and the individual SSW event. At one station (Davis, 69°S, 78°E), GW variance was reduced by ~ 50%, while at Syowa (69°S, 40°E) there was an increase of ~ 20% in variance.

All the studies cited above analyzed either data from a single or limited locations or 91 a global dataset but with a very sparse spatial coverage (note that the CHAMP data 92 has only  $\sim$  one hundred or so occultations per day). In addition, those CHAMP GPS 93 studies analyzed the global data only below  $\sim 35$  km. In comparison, the COSMIC data 94 processed by the University Corporation for Atmospheric Research (UCAR)'s COSMIC 95 Data Analysis and Archive Center (CDAAC) has a ten-fold increase of daily occultations 96 [Rocken et al., 2000] and the temperature retrievals reach an altitude as high as 60 km. The 97 UCAR CDAAC has also reprocessed the CHAMP GPS data with an altitude range from 98 near the ground up to 60 km. In this study, we use both the UCAR CDAAC COSMIC and 99 CHAMP GPS temperature retrievals between 20 and 60 km to examine SSWs occurring 100 during the 2007/08 Northern Hemisphere winter and to analyze the corresponding GW 101 characteristics so that we can gain some understanding of the interactions between SSWs 102 and GWs for this particular season. Since this is the first study to utilize the COSMIC 103 and CHAMP GPS temperature data above 35 km in altitude, independent temperature 104 retrievals from HIRDLS and SABER are used to supplement and validate the GPS analysis 105 at upper levels. 106

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The paper is organized as follows. Section 2 describes the datasets used in this study. Sections 3 and 4 show the temporal variability of zonal mean temperatures and zonal mean GW temperature amplitudes at high latitudes. Section 5 discusses the geographic variability of GW amplitudes. A GW ray-tracing experiment is presented in Section 6 to interpret the observed temporal variability of GW amplitudes in the stratosphere. In the end, the summary and conclusions are given.

### 2. Data

The concept of atmospheric profiling by GPS radio occultation (RO) was first introduced 113 by Yunck et al. [1988]. GPS RO is a space-borne remote sensing technique providing 114 accurate, all-weather, high vertical resolution profiles of atmospheric variables. Satellites 115 in low-Earth orbit (LEO), as they rise and set relative to the GPS satellites, measure 116 the frequency change of the GPS dual-frequency signals. The Doppler-shifted frequency 117 measurements are used to compute the bending angles of the radio waves, which are 118 reduced to derive the atmospheric refractivity. In the neutral atmosphere, the refractivity 119 is further reduced to temperature, pressure and water vapor profiles. GPS/MET was 120 the first demonstration of the GPS RO technique [Ware et al., 1996]. There were a few 121 follow-on GPS experiments. They include the German Challenging Minisatellite Payload 122 (CHAMP) and the Argentine Satellite de Aplicaciones Cientificas-C (SAC-C) missions 123 both of which were launched in 2000. Most recently, the Constellation Observing System 124 for Meteorology Ionosphere and Climate (COSMIC)/Formosa Satellite 3 (FORMOSAT-3) 125 [Rocken et al., 2000] was successfully launched into orbit in April 2006. Compared with 126 previous GPS missions, COSMIC provides an unprecedentedly large number of radio 127 occultations. Since the pioneering work of Tsuda et al. [2000], various authors have used 128

those different GPS datasets to study stratospheric GWs [e.g., de la Torre et al., 2004;
Ratnam et al., 2004; Baumgaertner and McDonald, 2007; Hei et al., 2008; and Alexander
et al., 2008].

In this study, we analyze the Version 2.0 COSMIC and CHAMP dry temperature profiles 132 processed by the UCAR CDAAC. We focus on the period from 1 December 2007 to 31 133 March 2008 when there were  $\sim 1500$  and 150 daily soundings from COSMIC and CHAMP, 134 respectively. Both COSMIC and CHAMP temperature data have a vertical resolution of 135  $\sim 1 \text{ km}$  and their accuracy is sub-Kelvin. Since COSMIC and CHAMP data have similar 136 data quality, we merge them to gain better spatial coverage. The locations of the merged 137 GPS daily RO occultations are roughly evenly distributed in space and local time and 138 their daily maximum latitude routinely reaches within  $2^{\circ}$  of the poles so the GPS data 139 are particularly useful for studying polar phenomena such as SSWs. Another advantage 140 of the GPS data (e.g., CHAMP and potentially COSMIC) is that they can have longer 141 temporal coverage than many other satellite data. The GPS RO retrievals are available 142 from near the ground up to 60 km but we analyze temperatures only above 20 km to 143 emphasize the stratosphere and lower mesosphere region. 144

To supplement and validate the GPS analysis especially at upper levels, we also use independent temperature retrievals from the EOS/HIRDLS [*Gille et al.*, 2008] (Version 4) and TIMED/SABER [*Mlynczak and Russell*, 1995] (Version L2A) when and where they overlap with the GPS data. All three datasets have global coverage, though SABER can sample only one hemisphere's high latitude region at a time due to the TIMED satellite's yaw cycle and the highest latitude that HIRDLS reaches is ~ 80°N. Also, relevant to the time period that we are studying, we miss quite a few days of data for HIRDLS. Unlike

GPS, both HIRDLS and SABER sample along single measurement tracks per orbit. Both 152 GPS and HIRDLS have a relatively high vertical resolution ( $\sim 1 \text{ km}$ ) so in theory they 153 can be used to study GWs of vertical wavelengths as short as 2 km. For HIRDLS, the 154 instrument field of view is 1.2 km, so the shortest wave may be closer to 2.4 km. Note that 155 in practice, it would be difficult to revolve waves with scales very close to the Nyquist 156 vertical wavelength mentioned above. Alexander el al. [2008] have used the HIRDLS 157 data to derive global estimates of GW momentum flux. SABER has a relatively coarser 158 vertical resolution of  $\sim 2$  km. 159

# 3. Temporal Variability of Zonal Mean Temperatures

Figure 1 shows the time-altitude contour of zonal average of daily mean GPS temperatures at 70°N (with a latitudinal bin of 10°) and time-latitude contour of zonal average of daily mean GPS temperatures at 10 hPa pressure level between 1 December 2007 and 31 March 2008. The time-latitude contour of zonal mean zonal wind analysis data from the European Centre for Medium-Range Weather Forecasts (ECMWF) (ds111.2) [*Trenberth*, 1993] is also shown in Figure 1.

The polar stratosphere was generally relatively quiet until late January when the strato-166 spheric temperatures warmed up quickly and several episodes of SSWs occurred. For 167 example, at 30 km in altitude, the zonal mean temperatures increased by more than 30 168 K within only a couple days before 25 January 2008. More episodes of dramatic strato-169 spheric temperature increase followed. We can clearly identify four SSW events. All of 170 them showed the classic downward progression of the warm stratospheric temperatures, 171 the accompanying mesospheric coolings (with little time difference between stratospheric 172 warmings and mesospheric coolings in those cases), the lowered stratopause height, the 173

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reversed meridional temperature gradient, and the weakening (or even reversal) of the 174 zonal wind. If we define the date of each event by the time when the meridional tem-175 perature gradient was positive and its value was maximum, the four SSWs occurred at 176 25 January, 2 February, 16 February, and 23 February of 2008, respectively. Among the 177 events, the 23 February one is a major event which is characterized by the reversal of the 178 zonal wind at 10 hPa. The 25 January event is extraordinary in that its temporal change 179 of temperatures is the largest among the four even though it is a minor one by the WMO 180 definition. From the ECMWF analysis geopotential height data (not shown), these SSWs 181 are mostly of the zonal wave-1 type, though also with some wave-2 component. 182

<sup>183</sup> Note that there could be large uncertainties in GPS temperature retrievals at upper <sup>184</sup> levels (above  $\sim 35$  km) due to noise and the residual ionospheric effects [*Kuo et al.*, <sup>185</sup> 2004]. As noted by *Kuo et al.* [2004] though, the residual ionospheric effects in the GPS <sup>186</sup> RO retrievals are the smallest during solar minimum at night time. Indeed, the time <sup>187</sup> period considered in this study happens to correspond to a solar minimum. Also, we have <sup>188</sup> conducted a separate zonal mean analysis of the night-time GPS data only and found <sup>189</sup> that the results are largely the same as those reported here.

The temperature retrievals at upper levels are also affected by *a priori* information used for the optimal estimation of bending angles and integration of the hydrostatic equation in the CDAAC GPS RO inversions. Specifically, the CDAAC uses the NCAR climatology described in Section 4 of [*Randel et al., 2002*] for the optimal estimation of bending angles and initialization of temperatures at 80 km to calculate the hydrostatic integral (Note that other GPS RO processing centers may use different climate models for those purposes.) The detailed descriptions of the optimal estimation of bending angles

and the hydrostatic integral applied at the CDAAC are given by Kuo et al. [2004] and 197 Lohmann [2005]. As a result of using a priori in the inversions, the temperature retrievals 198 are a mixture of real neutral atmospheric signals, a priori information, and noise and 199 the residual ionospheric effects (as discussed above), and the relative contribution from 200 a priori increases significantly with altitude. Hence, the temperature retrievals at upper 201 levels can be severely diluted by a priori information. Since the temporal variability of 202 temperatures at upper levels exhibits a time scale of from several days up to  $\sim$  a week 203 during SSWs (Figure 1a) whereas the time scale of a priori used by the CDAAC is on the 204 order of a month, the temporal variability of zonal mean temperatures at upper levels is 205 likely due to true geophysical signals. 206

It would be interesting to compare the GPS results with those from HIRDLS and 207 SABER (Figure 2). Since HIRDLS data are reported at pressure levels while SABER data 208 are reported at geometric altitudes, the comparison is made at pressure and altitude levels 209 for them, respectively (the GPS products include both altitude and pressure information). 210 For the comparison with HIRDLS, we interpolate the GPS data to the HIRDLS pressure 211 levels (which have an equivalent pressure altitude resolution of  $\sim 0.672$  km if a pressure 212 scale height of 7 km is assumed) before calculating their differences shown in Figure 2b. 213 For the comparison with SABER, we interpolate both the SABER and GPS data linearly 214 to a regular vertical resolution of 1 km before calculating their differences shown in Figure 215 2d. Note that there datasets used in the daily and zonal mean analysis shown in Figure 216 2 have different spatial and local-time sampling. It is evident that all three datasets are 217 capable of capturing the SSW events in the stratosphere and to first order the temporal 218 variability of the GPS data at upper levels is generally similar to those from the other 219

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two datasets. Note that HIRDLS global mean temperatures are known to have a cold 220 bias at upper levels [Gille et al., 2008]. This could possibly explain the overall warmer 221 GPS temperatures than HIRDLS at upper levels. It is interesting to note that the GPS 222 RO zonal mean temperatures are somewhat less sensitive to warmings than HIRDLS and 223 SABER and this could be due to the optimization applied in the GPS RO inversions, that 224 dilutes the neutral atmosphere signals with a priori as discussed above. Nevertheless, the 225 comparison among the datasets suggests that the temporal variability of GPS zonal mean 226 temperatures at upper levels is realistic. 227

Finally, to assess the contribution of the real neutral atmospheric signals to the GPS 228 temperature retrievals used in this study, we analyze the "zmwy" parameter in the 229 CDAAC products. "zmwv" is the median height of the weighting vector for the ob-230 servational bending angle and at this height there is 50% of a priori in the optimized 231 bending angle (Sergey Sokolovskiy, personal communication). This parameter varies with 232 each individual RO occultation and for the occultations used in the analysis in Figure 233 1a, it varies mostly between 40 and 50 km with a mean value of  $\sim$  44 km. We have 234 also noticed that the value of "zmwv" is generally larger at high latitudes in winter (not 235 shown). This factor together with the better spatial coverage of the GPS RO data in the 236 polar regions than other satellite data (as described in Section 2) makes the GPS RO data 237 valuable for studying the polar middle atmosphere. 238

# 4. Temporal Variability of Gravity Wave Amplitude

As mentioned in Section 2, both GPS and HIRDLS have a rather good vertical resolution, so they can be used to study small-scale phenomena such as GWs. GW analysis depends on the extraction of GW perturbations, i.e., the removal of the "background".

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Previous studies estimated GW temperature perturbations by applying a vertical wave-242 length  $(\lambda_z)$  filter directly to individual GPS temperature profiles [*Tsuda et al.*, 2000; 243 Ratnam et al., 2004; de la Torre et al., 2004; Baumgaertner and McDonald, 2007]. In 244 fact, large-scale waves such as Kelvin waves can have similar  $\lambda_z$  as GWs. For example, 245 Holton et al. [2001] identified from radiosonde data Kelvin waves of zonal wavenumber 2 246 and 4 with vertical wavelength of  $\sim 4.5$  km and 3-4.5 km, respectively. Therefore, filtering 247 temperature profiles with respect to  $\lambda_z$  alone does not clearly separate global-scale waves 248 and GW signals. The combined COSMIC and CHAMP data provide nearly ten times 249 more daily profiles than previous GPS missions, thus giving us the opportunity to define 250 the background temperature on the basis of horizontal scale and to separate the GWs 251 from the global-scale waves on this basis. 252

We obtain GW perturbations using the following procedure (which is analogous to 253 Alexander et al., 2008). First, each profile is interpolated in altitude to a regular 200-254 m resolution (which is oversampling for both GPS and HIRDLS). Next, each day's 255 profiles are gridded to  $15^{\circ} \times 10^{\circ}$  longitude and latitude resolution. The S-transform 256 is performed as a function of longitude for each latitude and each altitude, giving zonal 257 wavenumber 0-12 as a function of longitude. Note that the S-transform is a continuous 258 wavelet-like analysis [Stockwell et al., 1996] that uses an absolute phase reference, and the 259 longitudinal integral of the transform recovers the Fourier transform. In this study we 260 reconstruct zonal wavenumbers 0-6 to define the "large-scale" temperature variation. This 261 large scale, interpolated back to the positions of the original profiles, is subtracted leaving 262 perturbations with horizontal fluctuations shorter than wavenumber 6. We have tested 263 the sensitivity of the analysis results using different cut-off zonal wavenumbers ranging 264

from 3 to 10 (whenever the data spatial coverage allows this) and have found that the major results reported here remain largely the same. Note that the above procedure to derive GW background profiles neglects any time variations of large-scale waves within one day. Finally, we derive GW temperature amplitudes as a function of altitude from the temperature perturbations using the S-transform.

Figure 3 shows the time (daily)-altitude contours of zonal averaged GW temperature 270 amplitudes at high latitudes. Evidently, there were enhancements of GW activity in the 271 stratosphere during SSWs. At 70°N, for example, GW temperature amplitude increased 272 by a factor of 3 on 25 January 2008 in comparison to the time when the atmosphere was 273 less disturbed during December 2007 and early January 2008. GW amplitudes were also 274 smaller after the late February major warming event when the polar middle atmosphere 275 started to transition from the winter to summer state. In the 25 January event, for in-276 stance, there was also a downward progression of GW signals associated with the warming 277 event (Figure 3d). 278

As mentioned in the Introduction, the enhancement of GW activity during SSWs has been reported in previous studies [e.g., *Duck et al.*, 1998; *Ratnam et al.*, 2004]. It is interesting though that the timing of GW enhancement was very close with that of the SSWs in the 2007/08 Northern Hemisphere winter (generally within 1 or 2 days) whereas *Ratnam et al.* [2004] reported enhanced GW potential energy appearing 10 days earlier than the major Southern Hemisphere SSW in late winter/spring of 2002.

We showed in Figure 3 GPS GW analysis no higher than 35 km in altitude. Figure 4 compares zonal mean GW temperature amplitudes as a function of time and vertical wavelength from both GPS and HIRDLS temperature retrievals at selected altitudes,

some of which are higher than 35 km. The temporal variability of GW amplitudes from 288 HIRDLS is rather consistent with that from GPS at lower altitudes (below  $\sim 35$  km) 289 and confirms the GPS observations that there was enhancement of GW amplitudes in the 290 stratosphere during SSWs. At 40 km and above, however, the two become opposite. 291 The GPS results continue to reveal larger GW amplitude during SSWs at upper levels but 292 the HIRDLS results show that GW amplitudes were subdued at upper levels in the lower 293 mesosphere during SSWs. Note that in Figure 4, 50 km was still in the upper stratosphere 294 except during the SSWs. 295

Bear in mind that we derive GW perturbations by removing large-scale zonal structures 296 reconstructed from the gravest zonal modes derived from the S-transform analysis, so the 297 GPS and HIRDLS GW analyses would be different if their respective zonal mode estimates 298 were different. Actually the amplitude and phase of the gravest zonal modes among the 200 various datasets are very consistent below  $\sim 40$  km but the GPS results are quite different 300 from those from HIRDLS and SABER at higher altitudes (not shown). To exclude the 301 possibility that such differences in zonal modes caused the differences in GW analysis, we 302 conduct a separate analysis using the conventional band-pass filter method (as by Tsuda 303 et al. [2000]) to derive GW perturbations for both GPS and HIRDLS (not shown), but 304 the results are the same. 305

The existence of GW critical-levels due to the reversal of zonal winds during SSWs act to block most GWs before they can reach the mesosphere, therefore we expect that there should be a reduction of GW signals in the mesosphere during SSWs [*Holton*, 1983]. Also, there has been direct observational evidence supporting this argument. For example, *Wang et al.* [2006] observed exceptionally strong GW signals in the stratosphere but very X - 16 WANG AND ALEXANDER: GRAVITY WAVE ACTIVITY DURING SSWS

week GW signals in the mesosphere in the course of an SSW event during the winter 311 MaCWAVE campaign. Thus, we have more confidence in the HIRDLS results at upper 312 levels, and it is likely that the small-scale variability shown in the GPS data above 35 km 313 might be due to the GPS retrieval uncertainty at upper levels. The residual ionospheric 314 effects are normally the largest source for GPS temperature retrieval uncertainties at high 315 altitudes [Kuo et al., 2004]. However, a separate GW analysis using only the night-time 316 GSP data to minimize the residual ionospheric effects still shows the same seemingly 317 erroneous temporal variability at upper levels. Also, if the small-scale variability is noise, 318 it is unclear why noise would increase during SSW events. Therefore further studies are 319 needed to pinpoint the underlying causes of the GPS retrieval uncertainty at upper levels. 320

# 5. Geographic Variability of Gravity Wave Amplitude

So far we have examined only the zonal mean temperatures and GW amplitudes. The 321 high horizontal resolution of the combined COSMIC/CHAMP dataset allows us to inves-322 tigate the geographic variability of GW amplitudes. Figure 5 shows the stereographic pro-323 jected contoured maps of GW amplitudes averaged between 30 and 35 km from the GPS 324 for the four days when the SSWs occurred. Also shown are the stereographic projected 325 contoured maps of daily mean zonal velocity components, wind speeds, and geopotential 326 heights at the 10 hPa pressure level from the ECMWF analysis. Here we use the wind 327 speed and geopotential height contours to identify the location of the polar vortex. The 328 polar vortex was generally well-defined except on 23 February 2008 when it was completely 329 broken down (which is characteristic of a major SSW). 330

All four days displayed large zonal asymmetry in GW amplitudes. In addition it appears that there is a fairly good correspondence between GW amplitudes and the strength of <sup>333</sup> polar vortex winds during weak warmings (top three rows): GWs were generally larger
<sup>334</sup> near the polar vortex edge and smaller in the vortex core and outside the vortex during
<sup>335</sup> SSWs. This observation does not hold for the major SSW when the polar vortex itself
<sup>336</sup> was poorly defined (bottom row). Such an association between larger GW amplitudes and
<sup>337</sup> the locations of polar vortex edges is also a normal feature during undisturbed conditions
<sup>338</sup> (not shown).

Some previous studies also examined the relationship between the polar vortex position 339 and GW activity during SSWs. For example, Duck et al. [2001] analyzed GW activity 340 from lidar temperature measurements over Eureka during the 1992/93 - 1997/98 winter-341 time campaigns and found high GW activity in the vortex jet after late December and 342 low GW activity in the vortex core, outside of the vortex altogether, and in the vortex 343 jet before mid-December. Ratnam et al. [2004] reported enhancement of GW energies 344 near the polar vortex edge and outside the polar vortex but weak GW energies inside 345 the vortex during the 2002 Southern Hemisphere major warming event. Except for some 346 differences in details, our results are generally consistent with those previous studies. 347

The association between larger stratospheric GW amplitudes and stronger winds (which often had a larger eastward component) in the same altitude range during most of the days examined is also observed in the stratospheric Aleutian high pressure system where winds were normally very weak and often had westward wind components. Those observations are likely evidence of selective transmission of GWs by the spatially varying background winds [Dunkerton and Butchart, 1984].

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#### 6. Mechanism for Stratospheric Gravity Wave Enhancements during SSWs

Figures 3 and 4 showed that GW amplitudes in the stratosphere were generally enhanced during SSWs. Such enhancements could be explained to some extent by the GW propagation considerations. During SSWs, the zonal wind reversal (or weakening) could refract GWs arising from the lower atmosphere in such a way that more waves could be observed by GPS and HIRDLS in the stratosphere (i.e., the so-called observational window effect introduced by *Alexander* [1998]). As the simplest illustration of this mechanism, we estimate the vertical wavelength of a stationary GW at the 10 hPa pressure level using the following formula

$$\lambda_z = 2\pi \frac{\overline{u}}{N} \tag{1}$$

where  $\lambda_z$  is vertical wavelength,  $\overline{u}$  is background zonal wind, and N is the background 354 buoyancy frequency. Equation (1) is a good approximation of the full dispersion relation 355 for zonally propagating stationary GWs. Figure 6 displays the daily time series of  $\lambda_z$ 356 calculated from this simplified dispersion relation using zonal mean zonal winds and N at 357 70°N from the Goddard Earth Observing System Version 5.0.1 (GEOS-5) analysis data 358 [*Rienecker et al.*, 2008]. Note that our analysis can resolve GWs with vertical scales no 359 shorter than twice the vertical resolution of the GPS and HIRDLS data ( $\sim 1 \text{ km}$ ). In 360 practice, the limited height range of the profiles means we cannot resolve GWs of ultra-361 long vertical scales, nor waves with scales very close to the Nyquist vertical wavelength. 362 Given this consideration and the results shown in Figure 4, it is reasonable to choose the 363 4-10 km vertical wavelength observational window for this particular analysis. Evidently, 364 Figure 6 demonstrates that the rapidly changing zonal winds during SSWs refract GWs 365 significantly and very rapidly to vertical scales that are most visible to the GPS and 366

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<sup>367</sup> HIRDLS observations. The estimated vertical wavelength for the third event is shorter
 than 4 km but still longer than the Nyquist vertical wavelength.

There is generally large zonal asymmetry in zonal winds in the polar winter middle 369 atmosphere and such zonal asymmetry can lead to the so-called GW selective transmission 370 effects discussed by *Dunkerton and Butchart* [1984]. Hence, we conduct a GW ray-tracing 371 experiment to see how both temporally and longitudinally varying zonal winds during 372 SSWs could affect GWs that fall into the observational window of the GPS and HIRDLS 373 data. In this experiment, we launch rays at an altitude of 10 km along the 70°N latitude 374 band with a longitudinal interval of 5°. We use a constant source spectra with zonal phase 375 speed ranging from -10 to  $10 \text{ ms}^{-1}$  with a resolution of  $0.2 \text{ ms}^{-1}$ . We choose such a narrow 376 band of phase speed centered around zero because Alexander and Rosenlof [2003] argued 377 that the GW source spectra in extratropics should be quasi-stationary in winter and fall 378 as constrained from satellite observations. The source spectra horizontal wavelength is 379 taken to be 300 km, being close to the statistics of GW parameters reported by Wang et 380 al. [2005]. The horizontal resolution of GPS RO temperature retrieval is  $\sim 150$  km along 381 the line-of-sight of the occultation path and  $\sim$  an order of magnitude small across the 382 path. Smoothed daily mean GEOS-5 analysis data are used to represent the background 383 atmosphere through which the waves are propagating. We use the Gravity-wave Regional 384 Or Global RAy Tracer (GROGRAT) [Marks and Eckermann, 1995] as the GW ray-tracing 385 solver. GROGRAT is capable of performing 4-D GW ray-tracing. For simplicity, only 386 vertical propagation is considered in this experiment. 387

Figure 7 shows the time series of the normalized probability of observing a GW in the altitude range of 25 to 35 km in the observational window of 4-10 km in vertical wavelength along the latitudinal band of 70°N. The probability is normalized in such a way that the maximum and minimum value of probability in the whole time series is linearly scaled to 1 and 0, respectively. The simulation results suggest that the GW propagation considerations alone could largely explain the enhanced stratospheric GW activity during SSWs. In addition, the propagation considerations can also explain the observed reduced GW amplitudes in the lower mesosphere, as mentioned above.

Another possible cause for GW temporal variability is the temporal variability of GW sources. GWs are spontaneously emitted when unbalanced flows are restored to a more balanced state, and the so-called spontaneous imbalance is one of the major sources of GWs, especially in the extratropics. Figure 8 shows the daily time series of mean GPS GW amplitudes between the altitude range of 20 and 25 km and north of 50°N. It also shows the daily time series of mean magnitudes of  $\Delta$ NBE at the 350 hPa pressure level between 50°N and 85°N.  $\Delta$ NBE is the residual of nonlinear balanced equation [*Zhang et al.*, 2001]:

$$\Delta \text{NBE} = 2J(u, v) + f\zeta - \nabla^2 \Phi - \beta u \tag{2}$$

where u and v are the zonal and meridional horizontal velocity component, respectively, 396 f is the Coriolis parameter,  $\beta$  is the meridional gradient of the Coriolis parameter,  $\Phi$  is 397 the geopotential height,  $\zeta$  is the relative vorticity, and J is the Jacobian term  $(J_{xy}(u, v) \equiv$ 398  $(\partial u/\partial x \cdot \partial v/\partial y) - (\partial v/\partial x \cdot \partial u/\partial y)$ . The above formula is derived from scale analysis 399 of the divergence equation and it can be shown that  $\Delta NBE$  should be zero if the flow 400 is perfectly balanced. The magnitude of  $\Delta NBE$  has been used as an indicator of GW 401 source regions in unbalanced flow [e.g., Zhang et al., 2001]. We evaluate  $\Delta NBE$  using 402 the GEOS-5 analysis data. The 350 hPa pressure level is where  $\Delta NBE$  is found to be 403

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the largest in the troposphere for this analysis. There is a significant correlation between 404 GW amplitudes and  $\Delta NBE$  (with a correlation coefficient of 0.42), but the two variables 405 do not exhibit high one to one correspondence as shown in Figure 8. Another likely GW 406 source in the polar winter is topography. We have evaluated the correlation between 407 the strength of low-level winds (as a crude proxy for the strength of topographic wave 408 source) from the GEOS-5 analysis data and stratospheric GW amplitudes and have found 409 that the two variables have an even lower correspondence (not shown). Obviously, GWs 410 can experience profound modulations and changes when they propagate away from their 411 sources, therefore it is difficult to separate source effects and propagation effects in those 412 simple correlational analyses. To understand fully the respective roles of wave sources and 413 propagation in causing the observed GW temporal variability, more detailed modeling 414 studies are needed. 415

#### 7. Summary and Conclusions

We investigate the stratospheric and lower mesospheric temperatures and GW ampli-416 tudes during the 2007/08 Northern Hemisphere winter using the COSMIC and CHAMP 417 GPS temperature retrievals and independent HIRDLS and SABER temperature data. 418 We identify four SSW events which occurred between late January to late February in 419 2008 (Figure 1). All the events showed the classic downward progression of warm strato-420 spheric temperatures, the accompanying mesospheric coolings, the lowered stratopause 421 heights, the reversed meridional temperature gradients, and the weakening or reversal (in 422 the case of the major warming event in late February) of the zonal winds. For the SSWs 423 examined in this study, there were little or no time lags between stratospheric warmings 424 and mesospheric coolings. 425

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We notice a large increase of GW amplitudes at high latitudes in the stratosphere 426 during SSWs in the 2007/08 Northern Hemisphere winter and the timing of the GW 427 enhancements with respect to SSWs was generally very close (within a couple days at 428 most) (Figures 3-4). Ratnam et al. [2004] also noted enhanced GW energies during an 429 SSW event in the Southern Hemisphere in 2002 but the stratospheric GW energy spike 430 occurred  $\sim$  ten days earlier than the warming event. The enhancements of stratospheric 431 GW activity during SSWs can be primarily explained by GW propagation considerations. 432 During SSWs, the zonal wind reversal (or weakening) could refract GWs arising from the 433 lower atmosphere in such a way that more waves could be observed by GPS and HIRDLS 434 in the stratosphere. The simple vertical wavelength estimates (Figure 6) and GW ray 435 tracing results (Figure 7) support this wave refraction interpretation. We also notice a 436 decrease of GW amplitudes in the lower mesosphere during SSWs (above  $\sim 35$  km, as the 437 stratopause is lowered during SSWs) (Figure 4). This reduction of GW activity is likely 438 due to the existence of GW critical levels caused by the zonal wind weakening or reversal 439 during SSWs, implying GW dissipation and drag on the mean flow at lower altitudes than 440 during undisturbed conditions. 441

Stratospheric GW amplitudes display large geographic variability. Consistent with some previous studies, GW amplitudes were generally larger at the polar vortex edge, and smaller in the vortex core and outside of the vortex. This association could be due to the possibility that strong polar vortex jet winds allow more transmission of GWs to this altitude range so that they can be discerned in the satellite data.

<sup>447</sup> As the first study to extend the usage of the COSMIC and CHAMP GPS temperature <sup>448</sup> data up to 60 km in altitude, we compare the GPS analysis with independent HIRDLS and

SABER temperature retrievals. We find that the temporal variability of the HIRDLS and 449 SABER zonal mean temperatures generally agrees well with that of the GPS (Figures 1 450 and 2) up to  $\sim 60$  km. This could have particular implications for polar atmospheric stud-451 ies because the GPS data have better coverage at very high latitudes (e.g., the COSMIC 452 GPS occultations can routinely reach within 2° of the poles) than other satellite data such 453 as HIRDLS and SABER. The GPS zonal mean temperatures are, however, somewhat less 454 sensitive to warmings than HIRDLS and SABER. GW analysis from GPS is consistent 455 with HIRDLS up to  $\sim 35$  km. At higher altitudes, there is indication that small-scale 456 variability in the GPS data is questionable, though this needs to be investigated further 457 in future studies. 458

We finally note that there exist different types of SSW events with various characteristics and more observational and modeling studies are needed to gain a more comprehensive and thorough understanding of the relationship between the two phenomena, which has significant implications for improved understanding of both the middle and lower atmosphere.

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Figure 1: Top: time-altitude contour of zonal mean GPS temperature at 70°N; Middle: time-latitude contour of zonal mean GPS temperature at 30 km; Bottom: time-pressure altitude contour of zonal mean zonal wind at 65°N from the ECMWF reanalysis. The red dashed lines mark the warming events identified. The black dashed line on the bottom panel marks the 10 hPa level.



Figure 2: Top left: time-pressure altitude contour of zonal mean temperatures from HIRDLS; Bottom left: time-altitude contour of SABER temperatures; Right column: temperature differences between HIRDLS/SABER and GPS.



Figure 3: Time-altitude contours of gravity wave amplitudes at 60, 70, and 80°N from GPS temperature retrievals. The lower-right panel shows the blowup contour image around the first minor warming event at 70°N.



Figure 4: Time-vertical wavelength contour of zonal mean gravity wave amplitude at  $70^{\circ}$  from GPS (left column) and HIRDLS (right column) at selected altitudes.



Figure 5: Stereographic projected daily mapped contour of gravity wave amplitude averaged between 30 and 35 km (left-most column) from GPS, and zonal velocity component (second column), wind speed (third column), and geopotential height (right-most cloumn) at 10 hPa from the ECMWF reanalysis. The four rows are for 25 January, 2 February, 16 February, and 23 February of 2008 (i.e., the four warming events identified in Figure 1), respectively.



Figure 6: Vertical wavelength of a zonally propagating stationary gravity wave derived from Equation (1). See text for more details.



Figure 7: Normalized probability of observing a GW with vertical wavelength between 4 and 10 km in the altitude range of 25 to 35 km from ray-tracing simulations using background winds and temperatures at 70°N derived from the GEOS-5 analysis data. A constant source spectrum with phase speed between -10 and 10 ms<sup>-1</sup> and horizontal wavelength of 100 km is used. The rays are launched at an altitude of 10 km. See text for more details.