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Helioseismic Holography of an Artificial Submerged Sound Speed Perturbation and Implications for the Detection of Pre-emergence Signatures of Active Regions

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Abstract We use a publicly available numerical wave-propagation simulation of Hartlep et al. (Solar Phys. 268, 321, 2011) to test the ability of helioseismic holography to detect signatures of a compact, fully submerged, 5 % sound-speed perturbation placed at a depth of 50 Mm within a solar model. We find that helioseismic holography employed in a nominal "lateral-vantage" or "deep-focus" geometry employing quadrants of an annular pupil can detect and characterize the perturbation. A number of tests of the methodology, including the use of a plane-parallel approximation, the definition of travel-time shifts, the use of different phase-speed filters, and changes to the pupils, are also performed. It is found that travel-time shifts made using Gabor-wavelet fitting are essentially identical to those derived from the phase of the Fourier transform of the cross-covariance functions. The errors in travel-time shifts caused by the plane-parallel approximation can be minimized to less than a second for the depths and fields of view considered here. Based on the measured strength of the mean travel-time signal of the perturbation, no substantial improvement in sensitivity is produced by varying the analysis procedure from the nominal methodology in conformance with expectations. The measured travel-time shifts are essentially unchanged by varying the profile of the phase-speed filter or omitting the filter entirely. The method remains maximally sensitive when applied with pupils that are wide quadrants, as opposed to narrower quadrants or with pupils composed of smaller arcs. We discuss the significance of these results for the recent controversy regarding suspected pre-emergence signatures of active regions.

Keywords Helioseismology, observations

1. Introduction

For almost two decades, helioseismic methods have been employed to search for evidence of magnetic flux rising through the convection zone (Braun, 1995; Chang, Chou,

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D.C. Braun (⊠) NWRA, CoRA Office, 3380 Mitchell Ln, Boulder, CO 80301, USA e-mail: dbraun@nwra.com and Sun, 1999; Jensen *et al.*, 2001; Zharkov and Thompson, 2008; Kosovichev, 2009; Hartlep *et al.*, 2011; Ilonidis, Zhao, and Kosovichev, 2011; Leka *et al.*, 2012; Birch *et al.*, 2012). Submerged magnetic fields may produce travel-time anomalies due to changes in the wave speed caused by the magnetic field or by the presence of flows and perturbations to the thermal structure associated with the magnetic field (Birch, Braun, and Fan, 2010). If positively identified, such signatures could play an important role in space-weather forecasting, and lead to a physical understanding of the emergence process, which is a key component of the solar-activity cycle. Recent detection of p-mode travel-time anomalies prior to the emergence of several large active regions, obtained with time–distance methods, have been reported (Ilonidis, Zhao, and Kosovichev 2011, 2012b), although no significant travel-time anomalies were subsequently measured from an independent analysis using helioseismic holography (Braun, 2012). Ilonidis, Zhao, and Kosovichev (2012a) suggest that this discrepancy may be due to differences in sensitivity between the methods employed.

Numerical simulations have provided artificial data through which helioseismic analysis and modeling can be tested (Jensen *et al.*, 2003; Benson, Stein, and Nordlund, 2006; Hanasoge *et al.*, 2006; Parchevsky and Kosovichev, 2007; Zhao *et al.*, 2007; Braun *et al.*, 2007; Cameron, Gizon, and Duvall, 2008; Parchevsky and Kosovichev, 2009; Crouch *et al.*, 2010; Cameron *et al.*, 2011; Birch *et al.*, 2011; Hartlep *et al.*, 2011; Braun *et al.*, 2012). Many of these simulations include near-surface flows, sound-speed perturbations, or magnetic structures typical of active regions or supergranulation. Simulations that propagate waves through completely submerged perturbations are rarer (Hartlep *et al.*, 2011), but are critical for testing and developing helioseismic methods that are sensitive to detect active regions prior to their emergence on the surface. In this work, we use one of the simulations of Hartlep *et al.* (2011) to test the sensitivity of helioseismic holography comparatively to subsurface sound-speed perturbations under a variety of applications.

2. Simulation

Hartlep *et al.* (2011) constructed a number of simulations containing p-modes propagating through a spherical domain containing localized perturbations of the sound speed about the standard solar Model S (Christensen-Dalsgaard et al., 1996). No flows or magnetic fields are included. The solar model is convectively stabilized by a neglect of the entropy gradient of the background model, which lowers the acoustic cutoff frequency. The mode amplitudes above 3.5 mHz are thus reduced in amplitude. In addition, the simulation is only populated with p-modes with angular degree [ℓ] between 0 and 170. The simulations span about 17 hours of solar time. A number of simulations using the same code are publicly available and include a variety of sound-speed perturbations at different depths. In this work, we employ the simulation with a peak 5 % sound-speed reduction at a depth of 50 Mm and with a horizontal size of 45 Mm (see Figure 1). The simulated velocity field is provided in arbitrary units and represented in heliographic coordinates, with 512 pixels in longitude and 256 pixels in latitude, and a cadence of one minute. The simulation is stored in a FITS file (sun.stanford.edu/~thartlep/Site/Artificial_Data/Entries/2012/3/21_Subsurface_sound_ speed_perturbations.html).

Our primary emphasis is on testing the ability of helioseismic holography to detect *p*mode travel-time signatures of the prescribed perturbation within the simulation, and to measure the *relative* sensitivity of the results (in both signal strength and background noise) to changes of methodology. In contrast, direct comparison of measured and expected travel times requires the computation and application of sensitivity functions, which is not attempted here. A prediction of the travel-time shift expected from a given sound-speed perturbation is a non-trivial exercise, but a rough estimate is useful. We estimate the travel-time



Figure 1 The sound-speed ratio $[c/c_0]$ in the simulation, where *c* is the perturbed sound speed and c_0 is the background sound speed of Model S (top panels), and the travel-time measurements (bottom panels) made with helioseismic holography using a "nominal" methodology (see text). (a) The variation with horizontal distance from the center of the circularly symmetric sound-speed ratio at a depth of 50 Mm below the surface of the simulation. (b) The variation with depth of the sound-speed ratio at the center of the perturbation. (c) The variation with horizontal distance of the azimuthally averaged mean travel-time shift measured using lateral-vantage helioseismic holography applied to the simulation at focus depths of 29.9 Mm (dotted line), 45.4 Mm (dash-dotted line), 54.4 Mm (solid line), and 64.5 Mm (long dashed line). The travel-time shift at the center of the perturbation as a function of focus depth. The error bars in panels (c) and (d) indicate the standard deviation of the realization noise determined from a region away from the perturbation (see text).

shift in the geometric-optics limit as the path integral of the fractional sound-speed perturbation (Equation (1) of Hartlep *et al.*, 2011) weighted by the inverse of the background sound speed in Model S. For convenience, the path is chosen as purely horizontal through the center of the perturbation. This procedure yields a travel-time increase of 23 seconds.

3. The Nominal Procedure and Results

Helioseismic holography (hereafter HH) is described extensively elsewhere (Lindsey and Braun, 1997, 2000, 2004; Chang *et al.*, 1997). For our purposes, it is useful to enumerate the data-analysis steps taken to define the "nominal," or baseline, procedure. This provides the context for investigating the sensitivity of the results to changes in methodology (discussed in Section 4).

The basic idea is to apply Green's functions to the solar oscillation field at the surface of the Sun (or in this case, a simulation) to estimate the amplitudes of incoming and outgoing waves at targets (or "focal points") at or below the surface. In the "lateral-vantage" or "deep-focus" configuration of HH (Lindsey and Braun, 2004; Braun, Birch, and Lindsey, 2004; Braun and Birch, 2008a), travel-time perturbations are extracted from the cross-covariances between these "ingression" and "egression" amplitudes with a focus below the surface (Figure 2).



Figure 2 Ray paths for *p*-modes converging on a focal point [f] that is 54.4 Mm below the surface of the spherical domain of the simulation (denoted by the thick solid line). The thinner solid lines denote rays spanning $\pm 45^{\circ}$ from the horizontal direction. This is the nominal range of impact angles for lateral-vantage HH. In Section 4.4 we perform HH with smaller ranges of impact angles. The dashed lines indicate the ray paths for impact angles spanning $\pm 7.5^{\circ}$ from the horizontal direction. The scale is in megameters.

To establish some common notation, we define the three-dimensional (3D) Fourier transform in time [t] and two spatial dimensions [x, y] of a function A(x, y, t) as $\hat{A}(k_x, k_y, \omega)$, where k_x and k_y are the horizontal wavenumber components and ω is the temporal frequency. We define the Fourier transform in only the temporal dimension of A as $\tilde{A}(x, y, \omega)$. Thus, the steps involved in the data analysis are as follows:

- i) The simulated surface velocity data, provided in heliographic coordinates, are remapped onto a Postel projection $\Psi(x, y, t)$. The nominal spacing of the Postel grid is $\delta x = \delta y = 8.54$ Mm (0.7°), which is the original spacing of the velocity data in heliographic coordinates. The central tangent point (x, y) = (0, 0) is defined as 34.2 Mm (2.8°) south of the location of the perturbation.
- ii) The 3D Fourier transform $[\hat{\Psi}(k_x, k_y, \omega)]$ of the Postel-projected data is computed in both spatial dimensions and in time. In the temporal-frequency domain, the data within a bandpass of 2.5 and 5.5 mHz are extracted for further analysis. The simulation contains very little *p*-mode power above 3.5 mHz.
- iii) A phase-speed filter is applied to $\hat{\Psi}$. The nominal method employs filters that are Gaussian in the phase speed $[w \equiv \omega/k \text{ (where } k^2 = k_x^2 + k_y^2)]$ for each depth with peak phase speeds $[w_0]$ and widths $[\delta w]$ specified in Table 1. In Section 4.3 we examine the sensitivity of the results to variations in the form of the filter.
- iv) A set of depths is chosen (Table 1) and Green's functions for both diverging $[G_{+}^{P}]$ and converging $[G_{-}^{P}]$ waves are computed in the same Postel-projected grid as the data (Lindsey and Braun, 2000). The Green's functions are multiplied by spatial masks defining a given pupil [P]. The nominal set of pupils represent quadrants (or "arcs") of annuli extending outward in four directions and are denoted E, W, N, and S. The annulus widths are determined by ray theory from the paths of acoustic modes diverging from the subsurface focus point and spanning a range of "impact angles" $\pm 45^{\circ}$ from the horizontal direction (see Figure 2). In Section 4.4 we explore the sensitivity of the results to narrower ranges of impact angles, and in Section 4.5 we employ different azimuthal extents of the pupil arcs.
- v) For each pupil quadrant [P], the ingression $[H_{-}^{P}]$ and egression $[H_{+}^{P}]$ amplitudes are estimated by convolutions of the data cube $[\Psi]$ with G_{-}^{P} and G_{+}^{P} , respectively, in both time and the two spatial coordinates. This is performed using a plane-parallel approximation by the simple product of \hat{G}_{+}^{P} and $\hat{\Psi}$ (Lindsey and Braun, 2000) in the 3D

Table 1 Dentities and a set					
filter parameters.	^z f [Mm]	Pupil Radii [Mm]	ℓ at 3 mHz	w_0 [km s ⁻¹]	δw [km s ⁻¹]
	29.9	16.0-128	124 – 175	74	37
	37.0	19.5 – 159	108 - 153	87	43
	45.4	24.4-190	95-134	96	49
	47.6	25.8-195	92-130	101	50
	49.9	27.1 - 209	89-126	105	52
	52.4	28.5-216	86-122	108	54
	54.4	29.2-224	84-119	111	55
	57.1	31.3-230	82-115	114	57
	59.2	32.0-237	79-113	117	58
	62.1	34.1-251	77 – 109	119	60
	64.5	36.2-254	75 - 106	122	62
	76.1	41.8-292	67-95	140	69
	87.9	48.0-327	60-85	153	77

Fourier domain. The validity and consequences of this approximation are explored in Section 4.1.

- vi) The cross-covariance functions between ingression and egression amplitudes corresponding to opposite quadrants (*e.g.*, E and W, N and S) are computed. The four resulting cross-covariance functions are summed.
- vii) Mean travel-time maps are determined from the sum of the four cross-covariance functions. The nominal method uses the "phase method" (Braun and Lindsey, 2000). In Section 4.2 we compare the phase method with results from fits of the cross-covariances to Gabor wavelets.
- viii) Maps of the mean travel-time shifts are determined from the residual of the travel-time maps after subtracting a two-dimensional (2D) polynomial fit to a "quiet Sun" area excluding the perturbation. As shown in Section 4.1 this procedure helps to remove the effects of the plane-parallel approximation used in step v).

Table 1 shows the pupil ranges for each selected focus depth z_f , determined from ray theory. Also listed are the range of mode degrees [ℓ] at 3 mHz, sampled by the pupil, and the parameters for the Gaussian phase-speed filter (see Section 4.3) at each depth. The highest value of ℓ at each depth represents waves propagating horizontally through the focal point, while the lowest value indicates modes which propagate at impact angles of $\pm 45^{\circ}$ from the horizontal direction (see Figure 2).

Figure 3 shows maps of the travel-time shifts for a sample of focus depths. The perturbation is clearly seen as an increase in travel-time shift with a maximum of between 15 and 20 seconds at the expected horizontal position. Figure 1c shows the azimuthal averages of the travel-time shifts for several focus depths while Figure 1d shows the variation of the travel-time shift at the center of the perturbation (hereafter "peak travel-time shift") with focus depth. It is clear that the horizontal and vertical dependences of the travel-time shifts reasonably characterize the shape of the perturbation.

We measure a background realization noise $[\sigma]$ as the standard deviation of the mean travel-time shifts within an annulus spanning distances 111 - 195 Mm from the center of the Postel projection. For the "nominal" maps shown in Figure 3, σ is about 2.1 seconds and does not vary substantially with depth. We find that the background noise for maps made at



Figure 3 Maps of the mean travel-time shift using the nominal methodology of lateral-vantage HH as applied to the Hartlep *et al.* simulation and for focus depths of (a) 29.9 Mm, (b) 37.0 Mm, (c) 45.4 Mm, (d) 54.4 Mm, (e) 64.5 Mm, and (f) 76.1 Mm. The grayscale indicates the travel-time shift in seconds.

different focus depths is correlated. For example, there is a correlation coefficient (measured after excluding a region around the perturbation) of 0.96 between maps made at 54.4 and 52.4 Mm, and a correlation of 0.56 between maps at 54.4 and 47.6 Mm.

4. Tests of the Methodology

4.1. Tests of the Plane-Parallel Approximation

In Section 3, step v, a convolution in time and horizontal spatial coordinates between the Green's functions G_{\pm}^{P} and the data Ψ is computed in the Fourier domain under the assumption that the functions G_{\pm}^{P} are invariant with respect to translation in the Postel coordinate frame (this assumption has been termed the "plane-parallel" approximation: Lindsey and Braun, 2000; Braun and Birch, 2008b). The use of this approximation is highly desirable, since it decreases computing time and resources by several orders of magnitude. For example, without its use, separate Green's functions for each target pixel would have to be computed, stored, accessed, and operated on with a 3D multiplication by the datacube in the computations.

A major result of this approximation is the introduction of a systematic bias in the mean travel-time shift, which is a function of the horizontal distance between the focus and the central tangent point of the Postel projection. The reason for this bias is straightforward: In the Postel (also known as azimuthal-equidistant) projection, distances measured along any line intersecting the central tangent point (hereafter simply called the "center") are accurate, but distances between all other points differ from their true great-circle values. Thus, a locus of constant phase of waves propagating either away from or towards the center is warped in the projected plane into an ellipse with the semi-minor axis aligned towards the center (Figure 4). These wavefronts do not match the assumed circular wavefronts (and pupils)



Figure 4 Examples of the distortion in wavefronts at the outer pupil boundaries centered on a target focus point (denoted by the plus sign) placed 188 Mm to the right of the center of the Postel projection, which is denoted by the \times symbol. The larger and smaller dotted circles show wavefronts at the outer pupil boundaries, as projected onto the Postel frame, for focus depths of 76.1 and 45.4 Mm, respectively. The solid circles show circular wavefronts as assumed in the plane-parallel approximation. The dotted and solid wavefronts coincide along the *x*-axis but deviate at other places, with the maximum deviation occurring at the top and bottom. The deviations are difficult to discern by eye in the left panel. The right panel shows a magnified version of the upper part of the left panel. The vertical line segments in the right panel indicate the length of the horizontal wavelengths of modes that propagate from the focus depth to the outer pupil boundaries.

of the computed Green's functions. For the depths and pupil parameters listed in Table 1 the distortion in distance is small compared to the horizontal wavelengths of the modes. For example, in Figure 4 are drawn wavefronts at the outer pupil boundaries (where the distortion is greatest) corresponding to focus positions placed 188 Mm (15.5°) to the right of the center and at depths of 45.4 and 76.1 Mm. The maximum distortion of the wavefronts for these depths is 2.3 and 3.6 Mm, respectively, and these values are small compared to the horizontal wavelengths (30 and 40 Mm) of the modes considered. However, the distortion in projected distances results in observable spurious mean travel-time variations that vary with the azimuthal angle of propagation from the focus as well as the distance between the focus and the wavefront. At the outer edge of the pupils these spurious shifts can be as large as 20-30 seconds. However, the net travel-time shift as assessed over the entire pupil is typically less than ten seconds over tangent-point distances below 200 Mm (*e.g.* see Figure 5).

To correct for this spatially varying bias, we fit and subtract a 2D polynomial to the raw mean travel-time maps (Section 3, step viii). A circular mask excluding the perturbation is applied before the polynomial fit. Figure 5 shows cuts through a mean travel-time map with and without this correction.

Since all of the distortions introduced by the plane-parallel approximation increase with tangent-point distance, it is worthwhile to test the approximation by computing travel-time shift maps with varying positions of the tangent point. A similar test was performed by Braun (2012) on solar observations, but comparing only measurements of realization noise. The simulation here provides a larger, isolated, signal that provides a complementary target for this type of test. Figure 6 shows that maps made using tangent points spaced 200 Mm apart, after correction for the bias discussed above, have residual differences on the order of a second. For smaller distances of approximately 20-30 Mm these residuals are well below a tenth of a second.



Figure 6 Maps of the mean travel-time shifts at a focus depth of 54.4 Mm and with the tangent point (center) of the Postel frame placed at the following locations: (a) centered on the perturbation, (b) 34 Mm to the north of the perturbation, and (c) 205 Mm to the north of the perturbation. (d) The difference between the maps shown in (c) and (a). The rightmost plots show horizontal (e) and vertical (f) cuts through the center of the perturbation of map (a) shown as solid lines and map (c) shown as dotted lines.

4.2. Comparisons of Travel-Time Measurements

As we note in Section 3 step vii, the mean travel times are determined from the sum of the cross-covariance functions. In the nominal procedure, there are four cross-covariances of the form

$$\tilde{C}^{\text{EW}}(\mathbf{r}, z_{\text{f}}, \omega) = \tilde{H}_{+}^{\text{E}}(\mathbf{r}, z_{\text{f}}, \omega) \tilde{H}_{-}^{W*}(\mathbf{r}, z_{\text{f}}, \omega), \qquad (1)$$

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where the asterisk denotes the complex conjugate, $\mathbf{r} = (x, y)$, and we have also included the dependence on focus depth z_f . The temporal Fourier transform of the sum

$$\tilde{C} = \tilde{C}^{\rm EW} + \tilde{C}^{\rm NS} + \tilde{C}^{\rm WE} + \tilde{C}^{\rm SN},\tag{2}$$

is used in the "phase method" (Braun and Lindsey, 2000; Braun and Birch, 2008b) to compute the mean travel time through

$$\tau_{\rm pm}(\mathbf{r}, z_{\rm f}) = \arg(\langle \tilde{C}(\mathbf{r}, z_{\rm f}, \omega) \rangle_{\Lambda \omega}) / \omega_0, \tag{3}$$

where the brackets indicate the average over the bandwidth $\Delta \omega$, and ω_0 is the mean frequency. The desired travel-time shift [δt] is obtained from τ_{pm} by subtracting a 2D polynomial fit to a quiet Sun region (step viii). A typical summed cross-covariance function, transformed back to the temporal domain, is shown in Figure 7.

An alternative method for extracting travel-time shifts is to fit the cross-covariance function to a Gabor wavelet:

$$g = A\cos(\omega_0[t - \tau_{\rm gf}])\exp\left(-\frac{1}{2}\left[\frac{t - \tau_{\rm en}}{\sigma}\right]^2\right)$$
(4)

where A, σ , and τ_{en} are the amplitude, width, and position of a Gaussian envelope, ω_0 is the mean frequency, and τ_{gf} is the (phase) travel time, which is used instead of τ_{pm} to determine the travel-time shift δt . We have applied MPFIT routines (Markwardt, 2009) to perform a nonlinear least-squares fitting of the summed cross-covariance functions to Gabor wavelets for a focus depth of 54.4 Mm. The initial guesses of τ_{gf} in the fits were based on the peak closest to t = 0 of the cross-covariance function. Figure 7 shows an example of the fit of a single cross-covariance. Figure 8 shows that there is remarkable agreement between the mean travel-time shifts as determined from the phase method and the Gabor fits. We note that fine tuning the initial guesses based on the peaks of the cross-covariance functions to the left (or right) of the central peak yields phase times $[\tau_{gf}]$ that agree to within a fraction of a second of the times obtained using the central peak minus (or plus) the period $[2\pi/\omega_0]$. Thus, due to statistical fluctuations in the mean frequency, maps made using fits to these peaks are noisier than maps made using the central peak.

4.3. Sensitivity to Different Phase-Speed Filters

In Section 3 step iii, a phase-speed filter is applied to the Fourier transform $\hat{\Psi}$ of the datacube. Phase-speed filters are widely used in both time–distance helioseismology (Duvall



Figure 8 Comparisons of maps of mean travel-time shifts for a focus depth of 54.4 Mm obtained (a) using the nominal method including the phase method for extracting travel times from the cross-covariance functions and (b) using fits to Gabor wavelets to the same cross-covariance functions in the temporal domain. No corrections for the bias introduced by the plane-parallel approximation have been performed here; rather, a simple mean has been subtracted from each map. (c) A scatter plot of the two maps, compared to a line with unit slope.

et al., 1997; Couvidat and Birch, 2006) and helioseismic holography (Braun and Birch, 2006). The nominal procedure for lateral-vantage HH uses Gaussian filters

$$\phi = \exp\left(-\frac{1}{2} \left[\frac{w - w_0}{\delta w}\right]^2\right) \tag{5}$$

with a peak phase speed $[w_0]$ and width $[\delta w]$ such that the square of the filter has values of one and one-half at the highest and lowest wavenumbers, respectively, at 3 mHz as listed in Table 1. The use of phase-speed filters reduces the noise contributed by convective (nonwave) motions as well as from *p*-modes outside the range of desired phase speeds. Recently, Ilonidis, Zhao, and Kosovichev (2012a, 2012b) claim that different types of filters can affect the measured strength of subsurface signatures of emerging active regions. We have compared results using the nominal Gaussian filter, results using a "flat-top" filter similar to that employed by Ilonidis, Zhao, and Kosovichev (2012a), and results using no phase-speed filter. Figures 9 and 10 show comparable peak travel-time shifts in the simulated perturbation between the three cases, although the flat-top filter may be somewhat less sensitive to the variation with depth of the perturbation. This is also confirmed by computing the correlation coefficient between maps for different depths. For example, travel-time shifts at focus depths of 54.4 and 64.5 have a correlation of 0.45 using the Gaussian filter, but 0.64 using the flattop filter. These correlation coefficients were computed with the perturbation masked out, so they measure correlations in the background realization noise. Consistently higher correlation coefficients for all of the flat-top filtered results over this depth range (45-65 Mm) are observed. In general, the use of either filter produces somewhat less noise (as determined from the standard deviation of the realization noise outside of the perturbation) than using no filter, as expected (see Figure 10d).

A restriction in the simulation to mode power below $\ell = 170$ means that the tests performed here are not sensitive to variations in the filter properties below w = 70 km s⁻¹. Nonetheless, our general findings are consistent with expectations based on experience analyzing solar data for lateral-vantage holography performed for similar focus depths.

4.4. Sensitivity to Different Quadrant Widths

We explored the effect of changes to the range of impact angles of p-modes interacting with the perturbation, by decreasing the pupil width from the nominal values in Table 1. New



Figure 9 Mean travel-time shift maps made for a focus depth of 54.4 Mm and different phase-speed filtering: (a) a Gaussian phase-speed filter, (b) a flat-top filter, and (c) no phase-speed filtering. (d) The square of the filter function for several filters used: dotted, dashed, and dot–dashed lines indicate the nominal Gaussian filters corresponding to focus depths of 45, 54.4, and 64.5 Mm, respectively. The solid line shows the flat-top filter used in this study. There is no *p*-mode power in the simulation to the left of the vertical gray line. Thus, the tests here are not sensitive to differences between the filters at these low phase speeds.

pupil widths were computed using ray theory for impact angle extrema of $\pm 25^{\circ}$, $\pm 15^{\circ}$, and $\pm 7.5^{\circ}$ at the focus depth of 54.4 Mm. Figure 2 shows rays corresponding to impact angles of the nominal $\pm 45^{\circ}$ and the smallest range, $\pm 7.5^{\circ}$, considered.

Figure 11 shows that there is no substantial change in the strength of the perturbation as the impact angle is changed, within the uncertainty specified by the background realization noise. This result is expected, since the travel-time shifts due to a simple sound-speed perturbation should not depend on impact angle. There is a slight increase of realization noise, which also appears to take on a more fine-scale oscillatory pattern, as the pupil quadrant widths are decreased (Figure 11b). This is likely a diffraction (side-lobe) artifact due to the narrow pupil. The widths of the pupils for these angles ($\pm 7.5^{\circ}$) are smaller than the horizontal wavelength of the modes. To resolve this fine structure, the travel-time shift maps shown in Figure 11 were made with a grid spacing of half of the nominal value, by applying a Fourier interpolation of the original data.



Figure 10 Mean travel-time shifts for different focus depths, averaged in annuli centered on the perturbation (as in Figure 1c), using three different types of phase-speed filtering: (a) the nominal Gaussian filters, (b) the flat-top filter, and (c) no filtering. The depths are 45.3 (dash-dotted line), 54.4 (solid line), and 64.5 Mm (long dashed line). Error bars represent the standard deviation [σ] of the background realization noise in a region surrounding the perturbation (see text). The variation of σ with focus depth is shown in panel (d) for the three cases: Gaussian (solid line), flat-top (dotted line), and no filter (dashed line).

4.5. Sensitivity to Pupil Arc Size

The advantage of using four quadrants to compute the ingression/egression cross-covariances derives primarily from the utility in making measurements sensitive to flows as well as perturbations producing mean (horizontal-direction-averaged) travel-time shifts (Gizon and Birch, 2005). Ilonidis, Zhao, and Kosovichev (2012a, 2012b) have proposed several refinements, for application to time–distance (hereafter TD) methods, for the detection of subsurface signatures of emerging active regions. These include: i) dividing the annulus into a greater number of opposing arc pairs (*i.e.*, 6, 8, 10, 12, and 14 arcs), ii) making multiple measurements with different angular orientations of each set of arcs, and iii) combining all of the TD cross-covariances made with the different arcs and their orientations before the determination of the travel times. There are four different orientations used for each arc configuration in this scheme, as each set of arcs is rotated one-quarter of the angular extent of an arc.

We explore similar procedures for HH using the simulation of Hartlep *et al.* (2011). The results here complement the tests made for HH on Doppler observations obtained with the



Figure 11 Mean travel-time shift maps made for a focus depth of 54.4 Mm and with different ranges of impact angle: (a) $\pm 45^{\circ}$ and (b) $\pm 7.5^{\circ}$. Both maps were made using the same flat-top filter shown in Figure 9. (c) Measurements of the mean travel-time shift in the perturbation against the maximum (absolute) impact angle. The filled circles show the peak shift; the diamonds show the average shift within a 25 Mm radius. Error bars denote the standard deviation of the realization noise, which is also plotted as a solid line.



Figure 12 Mean travel-time shifts at a focus depth of 54.4 Mm from HH using different pupil geometries: (a) the nominal method using a fixed set of four quadrant pupils, (b) using six arcs and four orientations, and (c) the combination of 6, 8, 10, 12, and 14 arc configurations with four orientations of each configuration. The flat-top filter shown in Figure 9 is used. (d) Azimuthal averages of the travel-time shift over annuli centered on the perturbation for the three maps shown in the three top panels: quadrants (dotted line), six arcs (dashed line), and combined 6-14 arcs (solid line). (e) Measurements of the mean travel-time shift in the perturbation and the background realization noise σ against the number of pupil arcs used. The filled circles show the peak shift, and the diamonds show the average shift within a 25 Mm radius. Error bars denote the standard deviation of the realization noise, which is also plotted as a solid line. (f) The correlation coefficient between travel-time shift maps made using six arcs and the other arc configurations.

MDI instrument by Braun (2012). Figure 12 shows some of our results for the measurements on the simulated perturbation. In general, the use of six arcs produces a weaker (by about 25 %) travel-time signature in the perturbation than using quadrants. A slight trend of a

decreasing signal strength with the number of arcs from 6 to 14 is also observed (Figure 12e), although the net decrease is within the background noise. The realization noise increases with the number of arcs used from about 1.4 seconds for the four orientations of the sixarc set to 2.5 seconds for the four orientations of the 14-arc set. These can be compared with the 2-second noise measured using the nominal quadrant method. These results are consistent with the increase in noise using smaller arcs observed by Braun (2012) using MDI data. The map made from combining all cross-covariances from all pupil-arc configurations and orientations has a realization noise of 1.9 seconds, which is essentially identical to the nominal (quadrant) map. It is significant that maps made with different arc lengths are highly correlated with each other (Figure 12f).

5. Conclusions

In summary, we find that helioseismic holography, as performed in the nominal lateralvantage configuration and using the plane-parallel approximation, is in conformance with expectations well suited for detecting and characterizing subsurface sound-speed perturbations of the kind included in the simulation of Hartlep *et al.* (2011) at depths of at least 50 Mm. Suitable caution should be exercised: these results follow from a single simulation, which may have different physics from real solar perturbations. Other limitations, such as the inclusion in the simulation of only a subset (in both temporal frequencies and wavenumbers) of known solar oscillations, are noted. However, we believe that generally the viability of HH for the detection of subsurface perturbations is substantially confirmed, particularly its ability to select for analysis the relevant set of modes passing through a localized target below the solar surface.

Furthermore, mindful of the caveats mentioned above, we find no evidence that the sensitivity of the procedure, as assessed by the mean travel-time shift at the expected position of the perturbation, is enhanced by the use of the flat-top filter or different pupils, as suggested in the critique by Ilonidis, Zhao, and Kosovichev (2012a) of the results of Braun (2012). Specifically, the holographic signatures are influenced little by the detailed profile of the phase-speed filter, and very little more by the lack of any such filter. We also find that holography remains maximally sensitive when applied with spatially extended pupils, as opposed to restricting or partitioning them. The main effect of partitioning the pupil to smaller arcs is, if anything, a reduction of the signature and the appearance of diffraction effects.

Gabor-wavelet fitting can be applied to helioseismic holography as it is with other timedistance techniques, and so this should not be regarded as a discriminating qualification against it. In the case of the simulation, the results are essentially identical to those of the phase-method and in conformance with expected travel-time shifts given the size and amplitude of the perturbation.

Our tests do not attempt to replicate the time–distance procedures applied by Ilonidis, Zhao, and Kosovichev (2011); thus, we draw no conclusion about the sensitivity of their own measurements to the changes in methodology that they advocate. In attempting to understand the discrepancies of the results between Ilonidis, Zhao, and Kosovichev (2011) and Braun (2012), we can reasonably infer that negative holography results suggest that the suspected perturbation is different than the simple sound-speed perturbation simulated by Hartlep *et al.* (2011). Furthermore, it seems that the use of the plane-parallel approximation can be ruled out as a contributing factor to the negative results of Braun (2012).

It is possible that the physics of the suspected signatures are such that, unlike a simple sound-speed perturbation, the use of narrow pupils or different filters may be critical. The signatures may also produce complicated changes to the cross-covariance functions, perhaps due to unknown effects of magnetic fields (Ilonidis, Zhao, and Kosovichev, 2012a). Further tests need to be performed on the relevant data. In our opinion, it is possible that the signatures of Ilonidis, Zhao, and Kosovichev (2011) may represent noise. We return to the point made by Braun (2012) suggesting the need for blind "hare-and-hound" tests as a minimal condition for the signatures of the signals found by Ilonidis, Zhao, and Kosovichev (2011) to be established as pre-emergence signatures of deeply submerged magnetic fields. Tests with simulated data on artificial perturbations such as those reported here provide the critical context under which similar analyses of solar observations may be understood. In general, the results presented here provide confidence in helioseismic holography as a useful method for probing submerged perturbations (Leka *et al.*, 2012; Birch *et al.*, 2012).

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